

# Investigation of Single-Particle Structure in $^{26}\text{Na}$ using the new SHARC Array

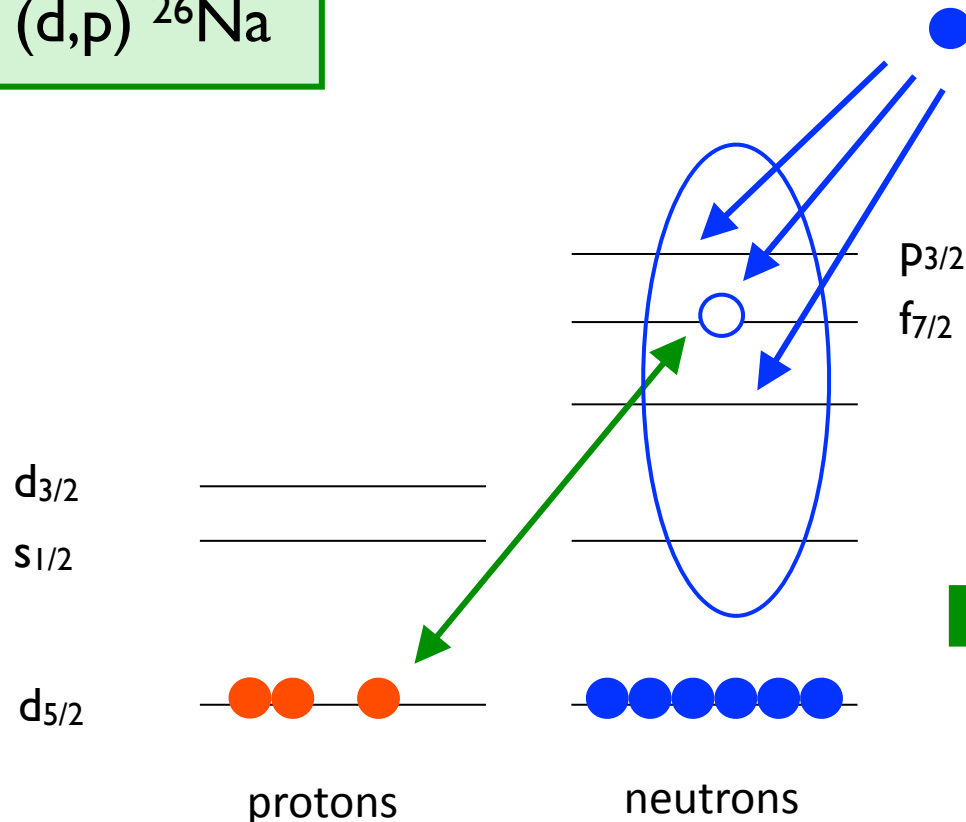
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Gemma Wilson



# Investigation of Single-Particle Structure in $^{26}\text{Na}$ using the new SHARC Array

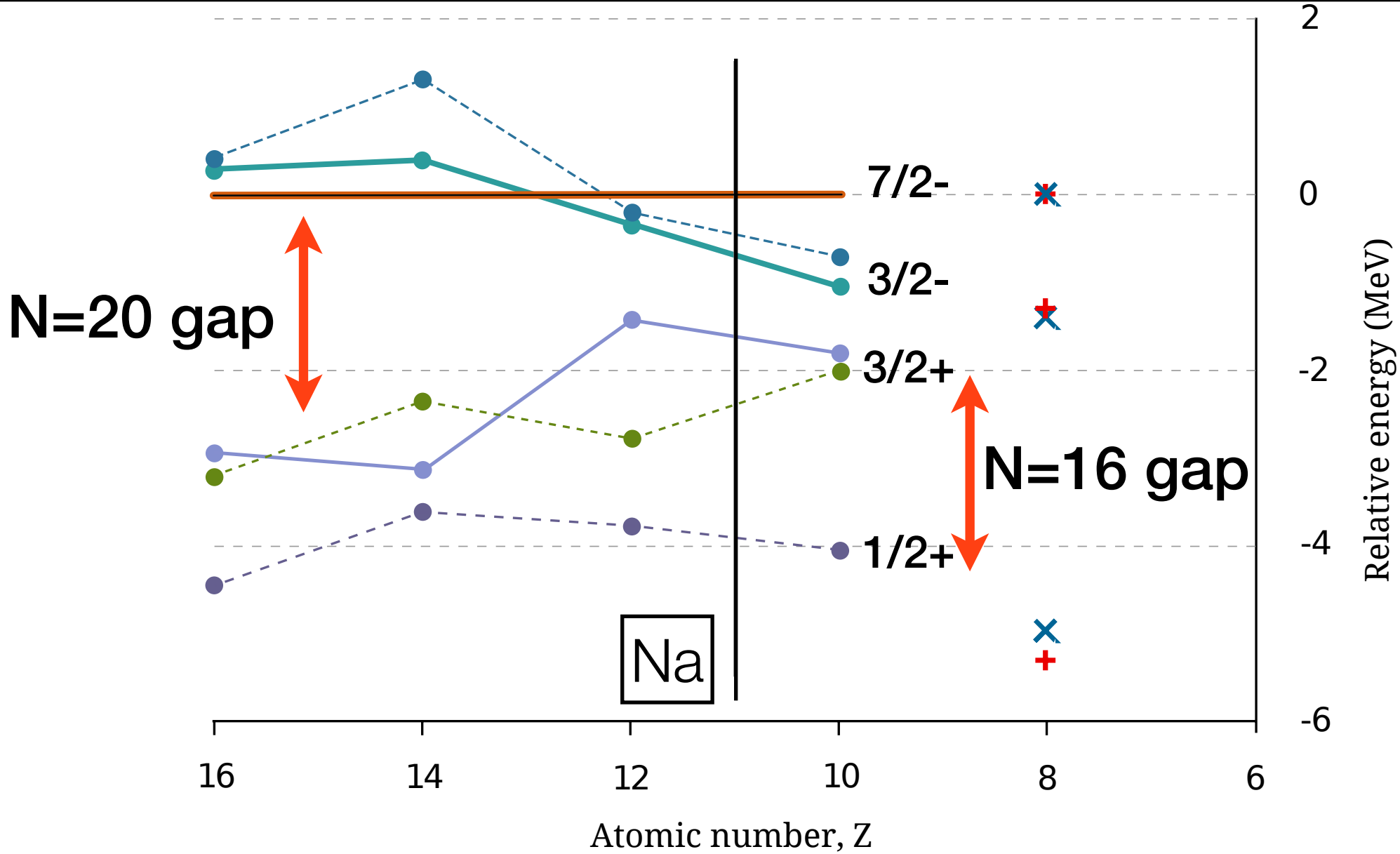
$^{25}\text{Na} (d,p) ^{26}\text{Na}$



Multiplets:  
 $\pi(d_{5/2}) \otimes \nu(p_{3/2})$   
 $\rightarrow (1, 2, 3, 4)^-$

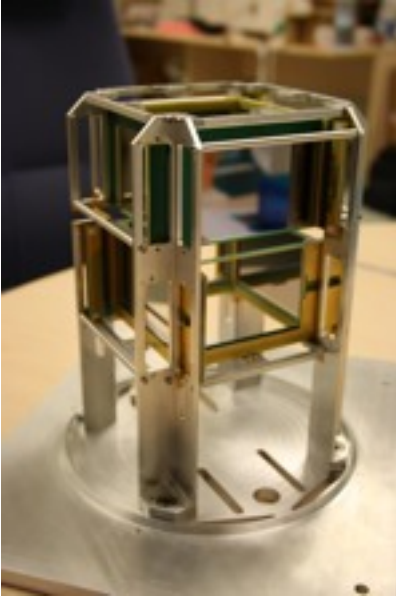
odd-odd final nucleus  
 High density of states  
 Gamma-gating needed

Migration of levels as nuclei become more exotic, normalised to 7/2- energy

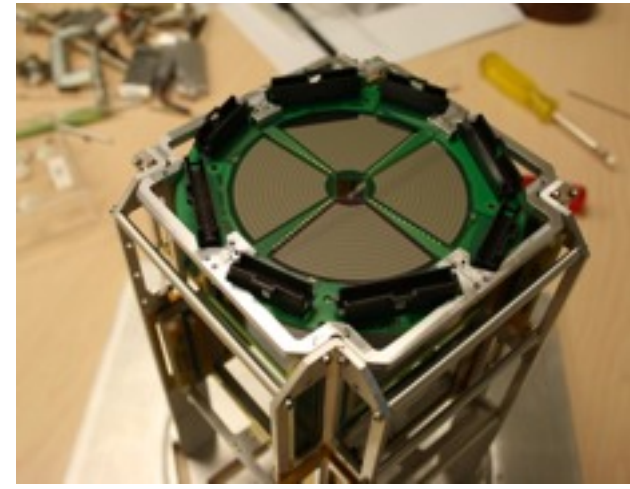


- 3/2-, N=15
- 3/2-, N=17
- Na, Z=11
- Dashed line: N=15
- Solid line: N=17
- 7/2-, N=15
- 7/2-, N=17
- 3/2+, N=15
- 3/2+, N=17
- ×  $^{21}\text{O}$ , N=13
- 1/2+, N=15
- 3/2+, N=17
- +  $^{23}\text{O}$ , N=15

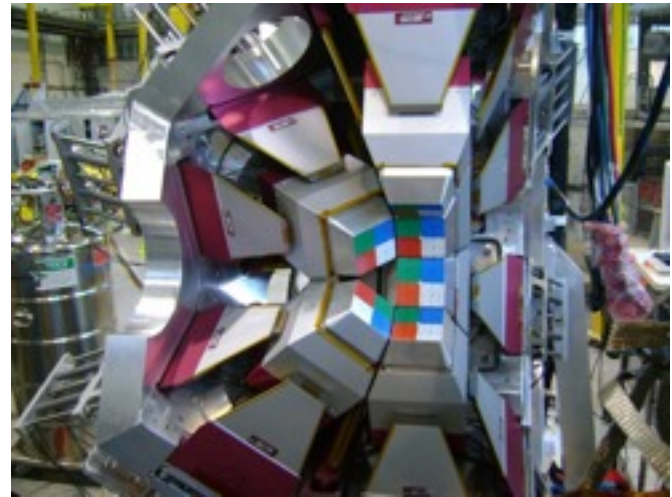
SHARC



- Upstream box of 4 DSSSDs
- Downstream box of up to 4 dE-E
- Upstream CD of 4 DSSSDs



- 4 clovers at 90°, 4 at 135°
- Full BGO suppression
- Each clover has 32-fold segmentation



TIGRESS

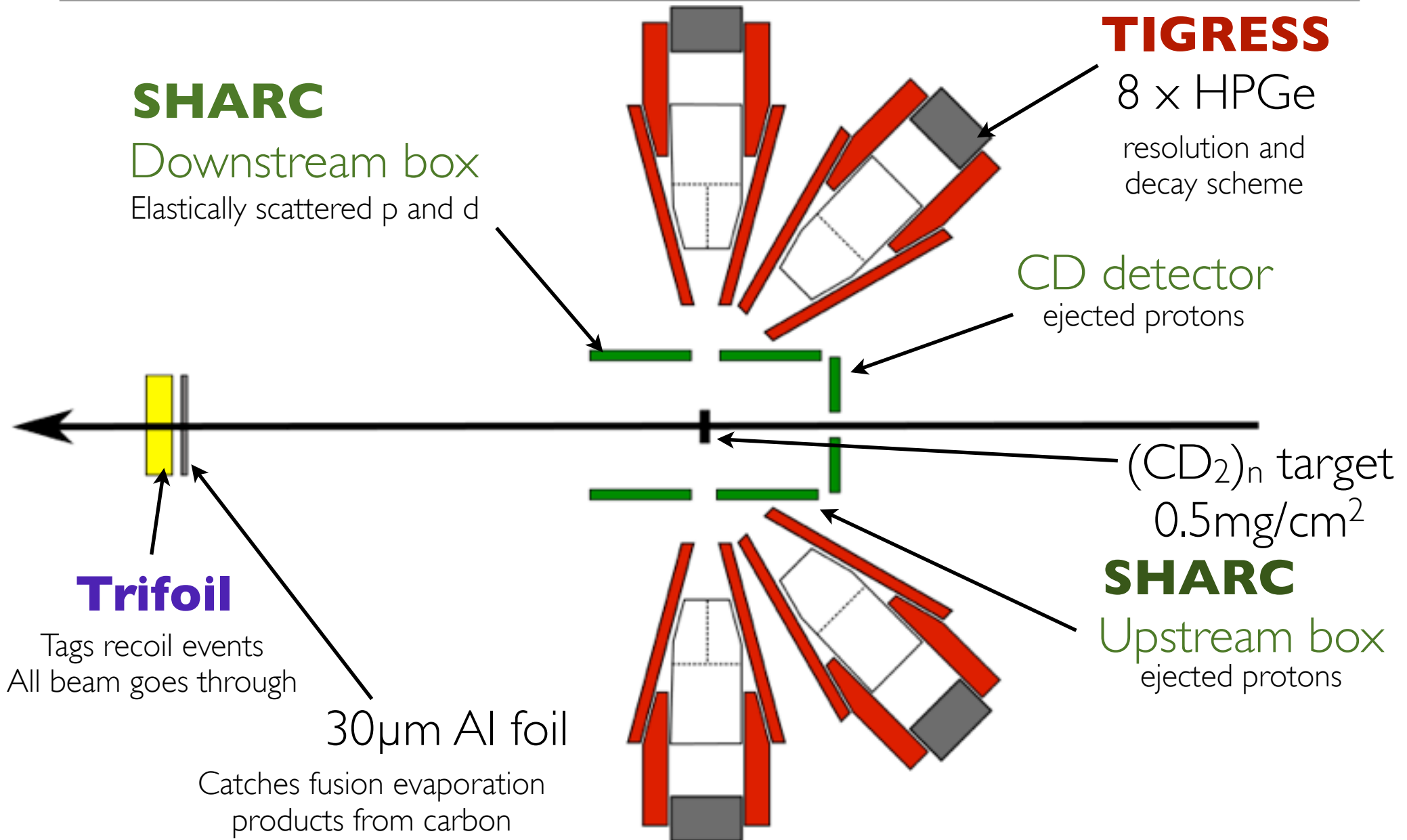
- Downstream of SHARC
- 10 $\mu$ m scintillation foil with active area of 40mm x 40mm
- Mounted with 30 $\mu$ m Al foil to stop fusion evaporation products

Trifoil

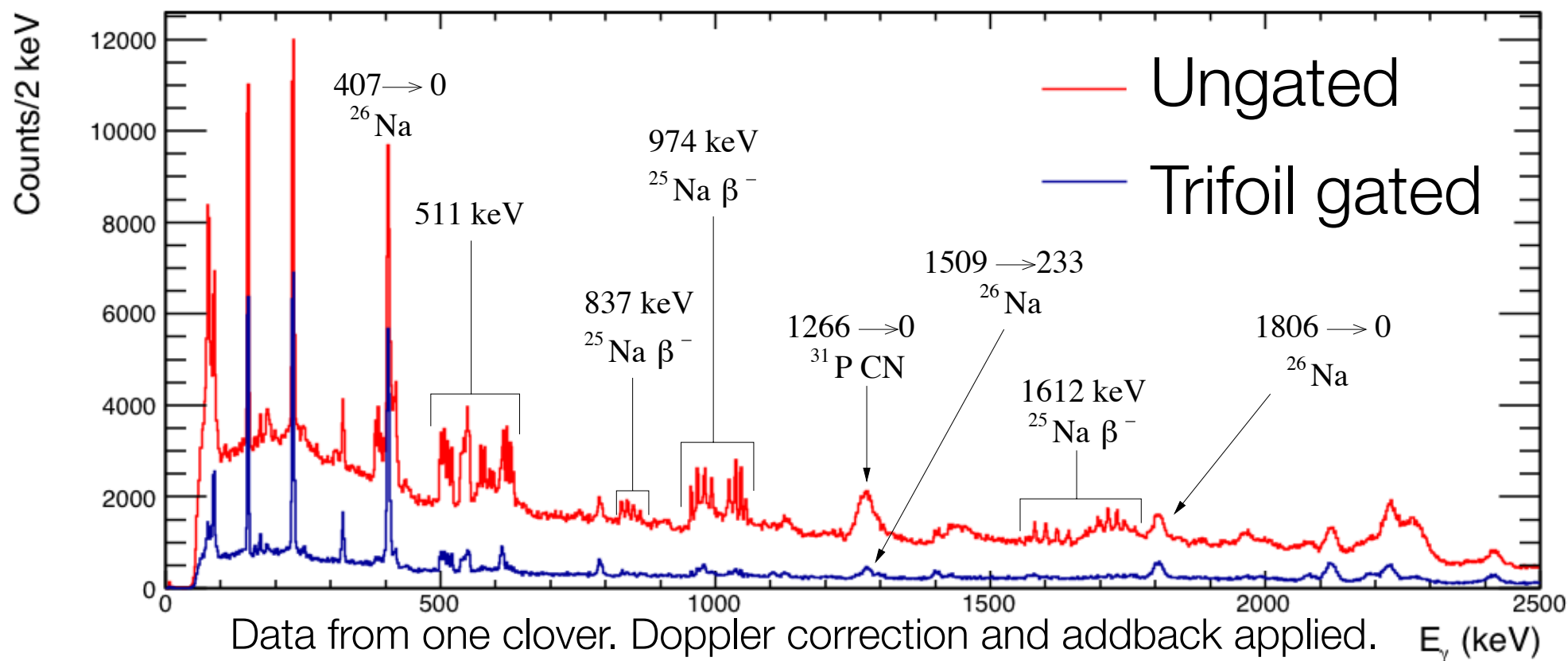


# Experimental Setup

$d(^{25}\text{Na},p)^{26}\text{Na}$  at TRIUMF  
Beam:  $3 \times 10^7$  pps,  
5 AMeV  $^{25}\text{Na}$  from ISAC II

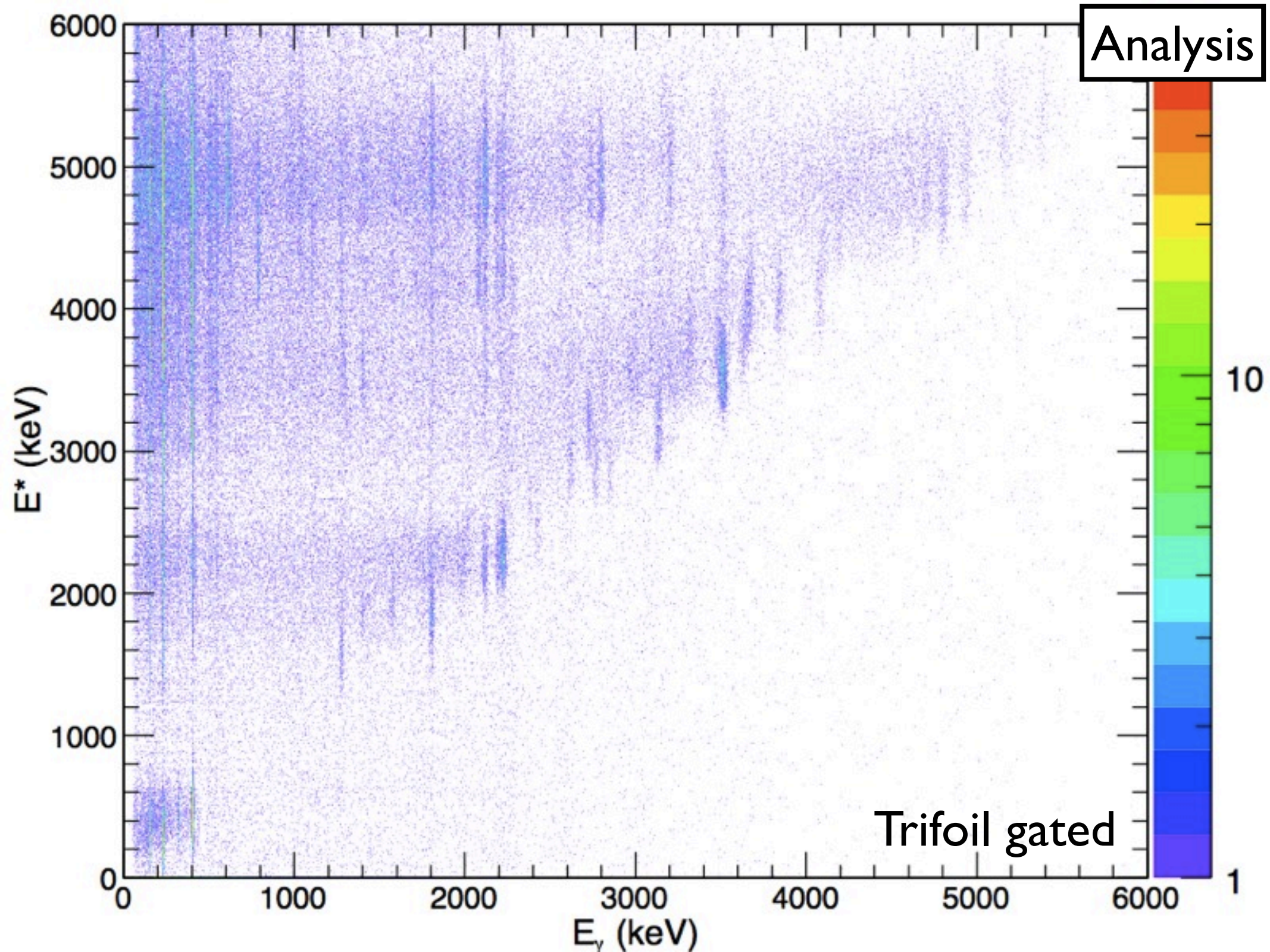


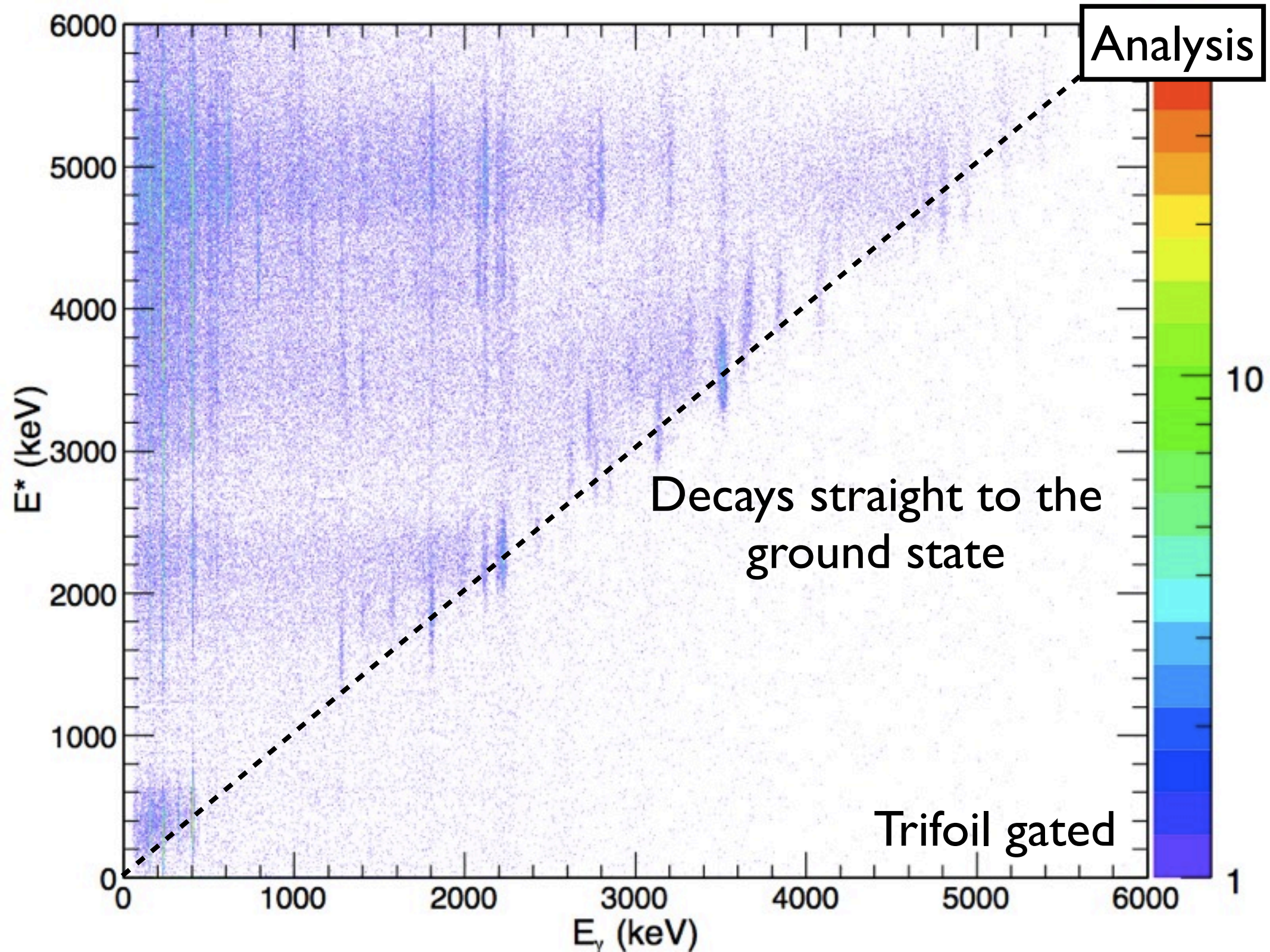
# Use of Trifoil for vetoing $\gamma$ rays



- signal to background ratio improved by a factor of 10
- 67% detection efficiency of  $\gamma$  rays from  $^{26}\text{Na}[1]$

[1] G.W. *et al.*, J. Phys. Conf. Ser. **381**, 012097 (2012)

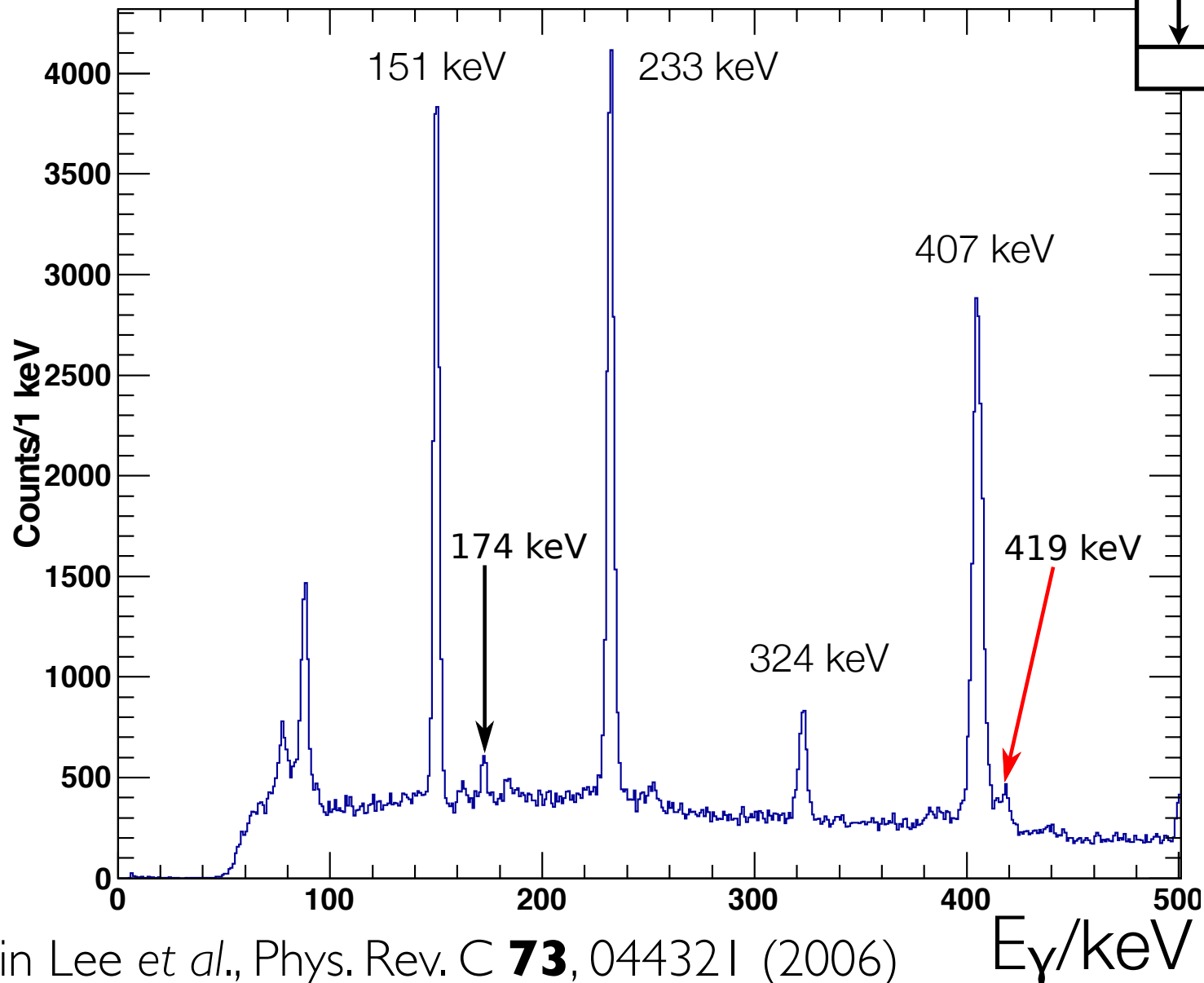






# Using the $E_x$ vs $E_\gamma$ plot to identify $\gamma$ rays

[1]

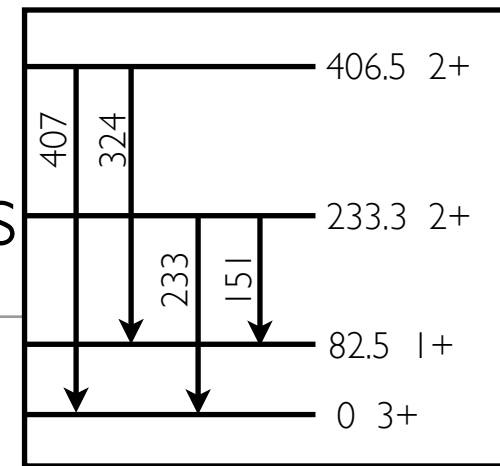


$^{26}\text{Na}$

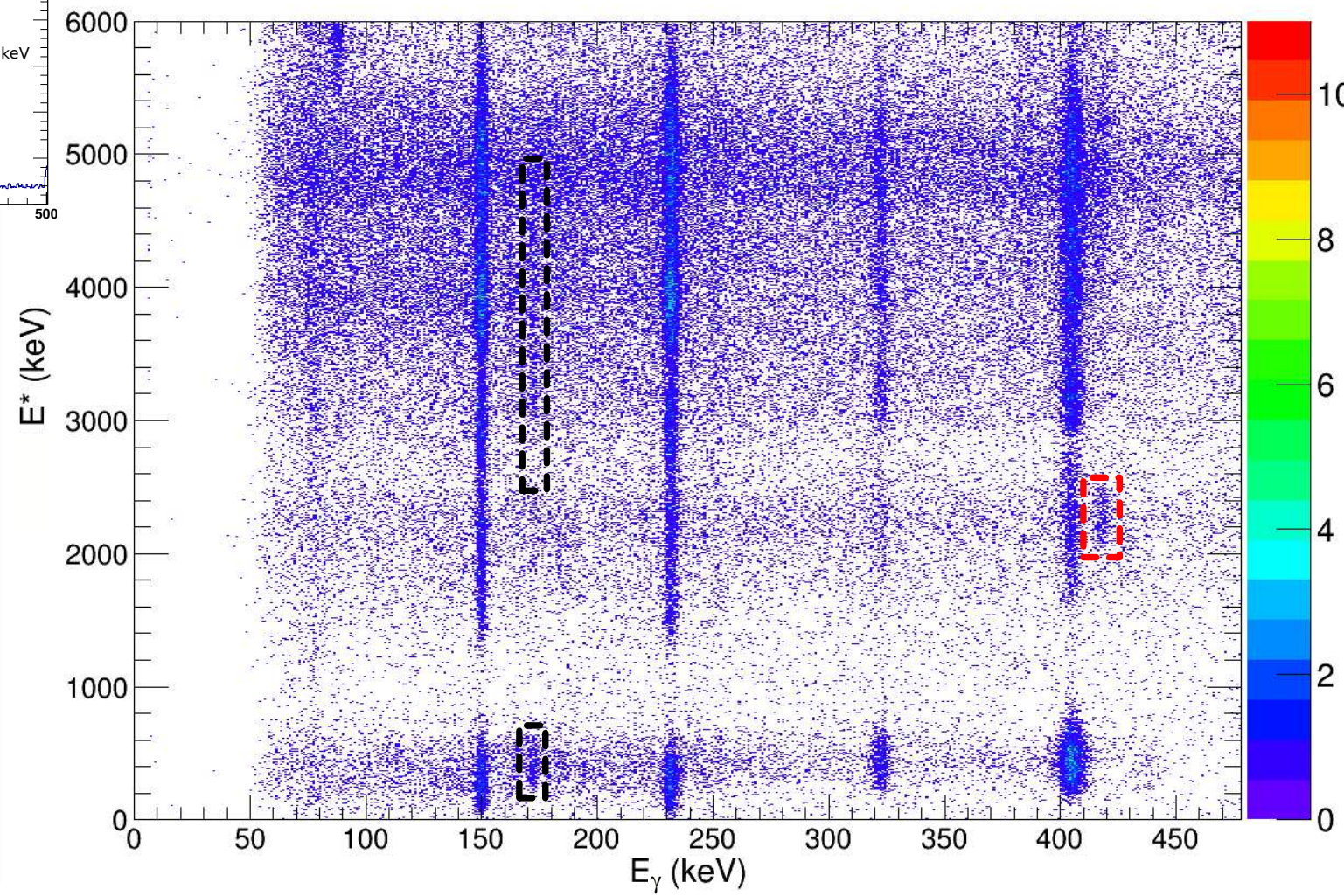
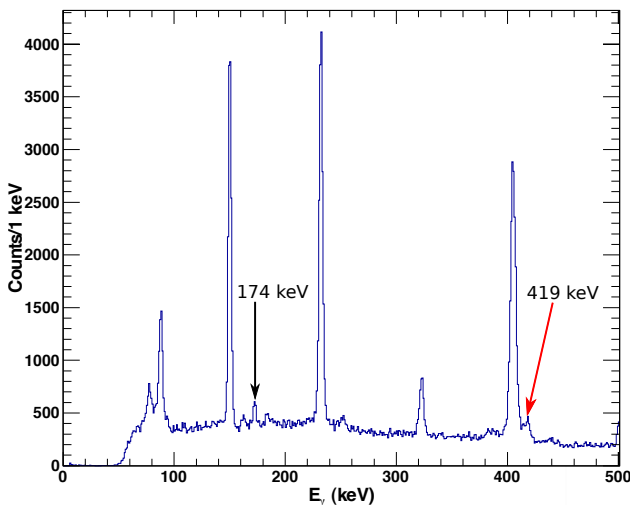
$E_\gamma/\text{keV}$

# Using the $E_x$ vs $E_\gamma$ plot to identify $\gamma$ rays

[1]

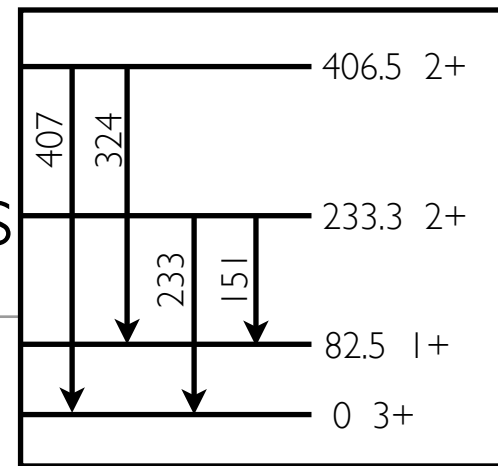


$^{26}\text{Na}$

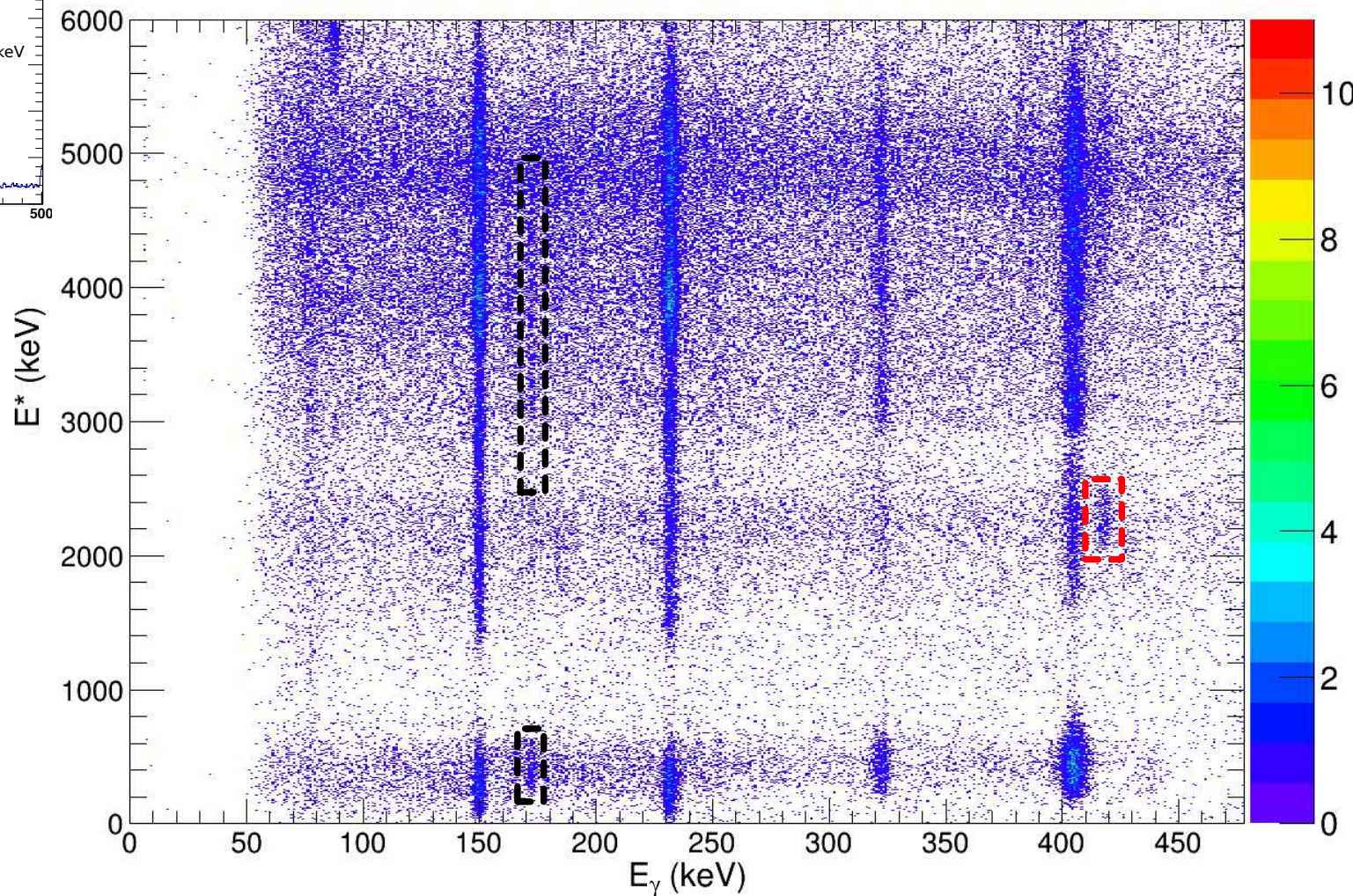
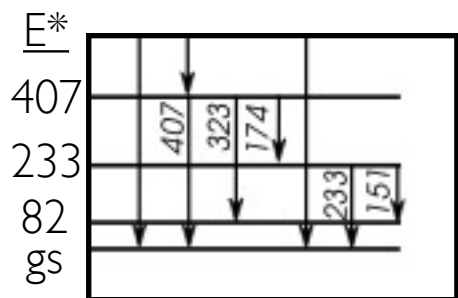
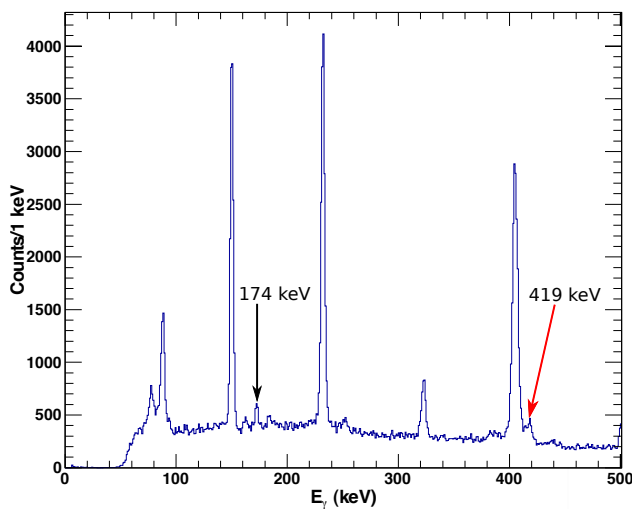


# Using the $E_x$ vs $E_\gamma$ plot to identify $\gamma$ rays

[1]

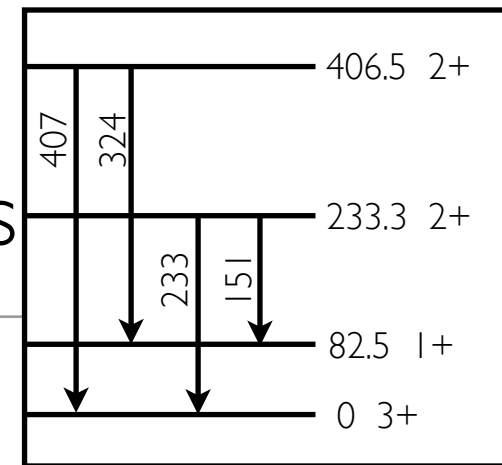


$^{26}\text{Na}$

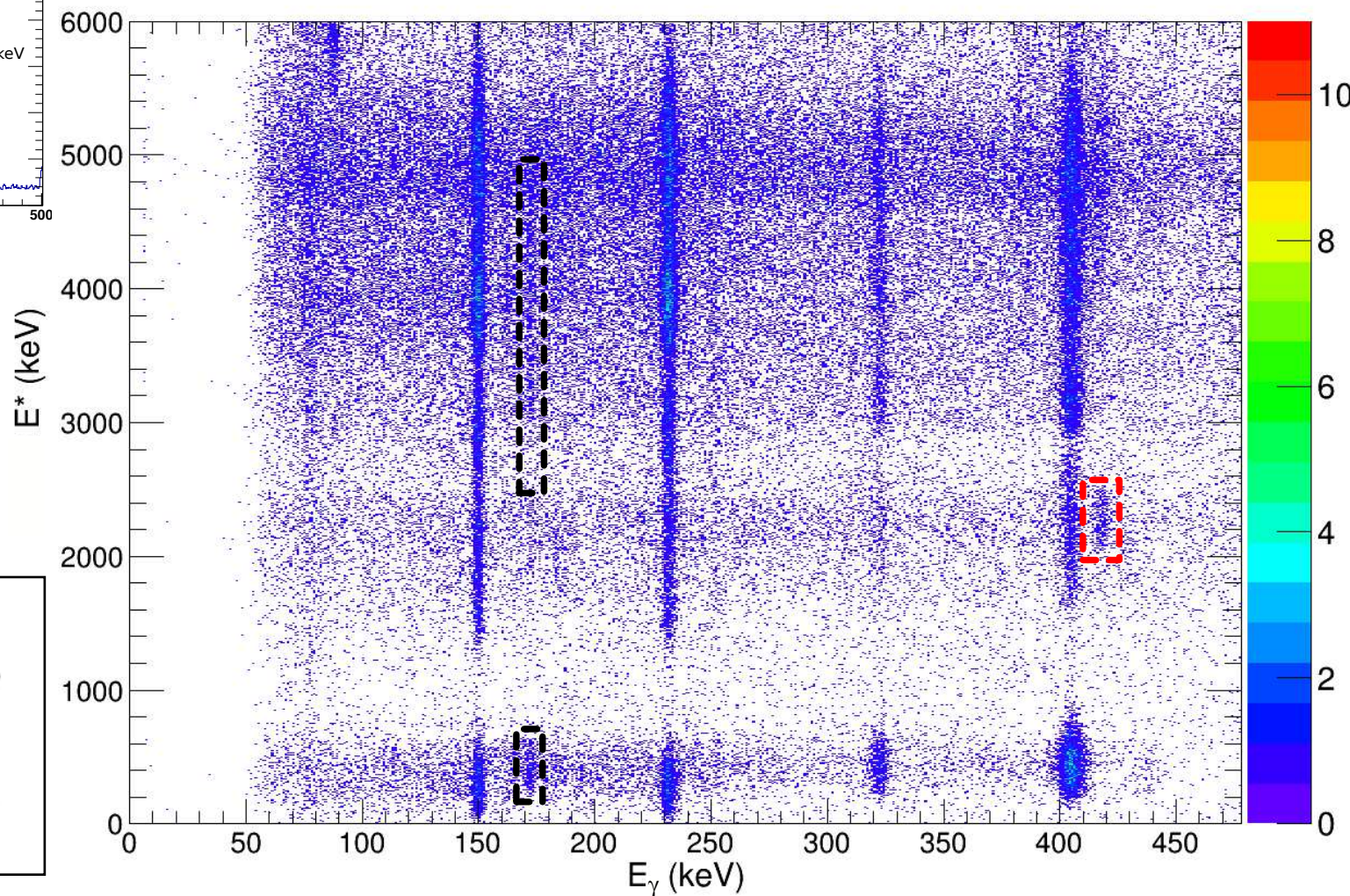
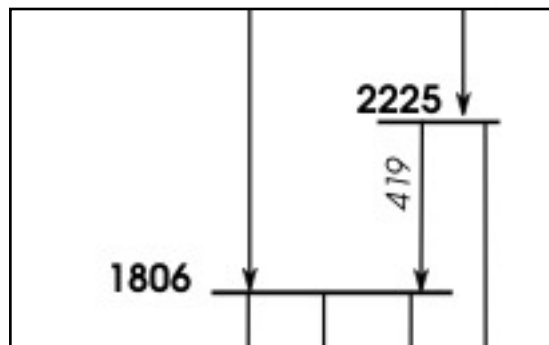
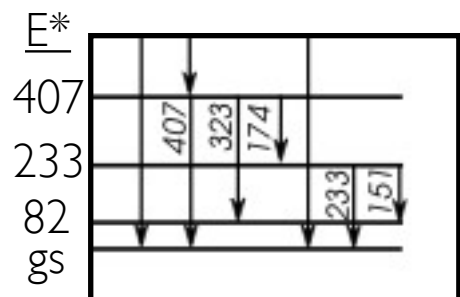
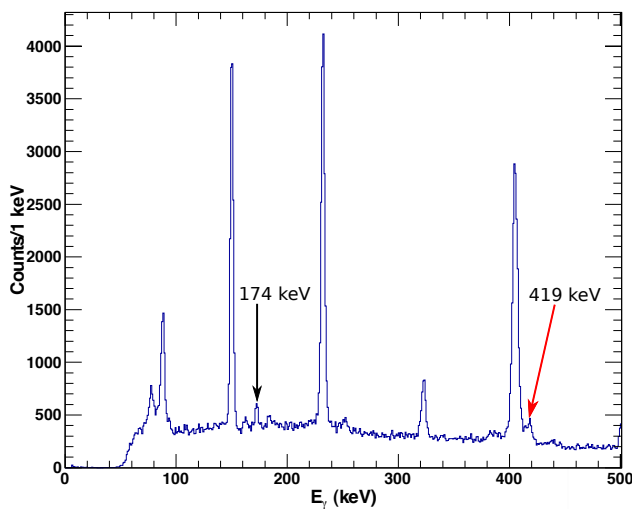


# Using the $E_x$ vs $E_\gamma$ plot to identify $\gamma$ rays

[1]



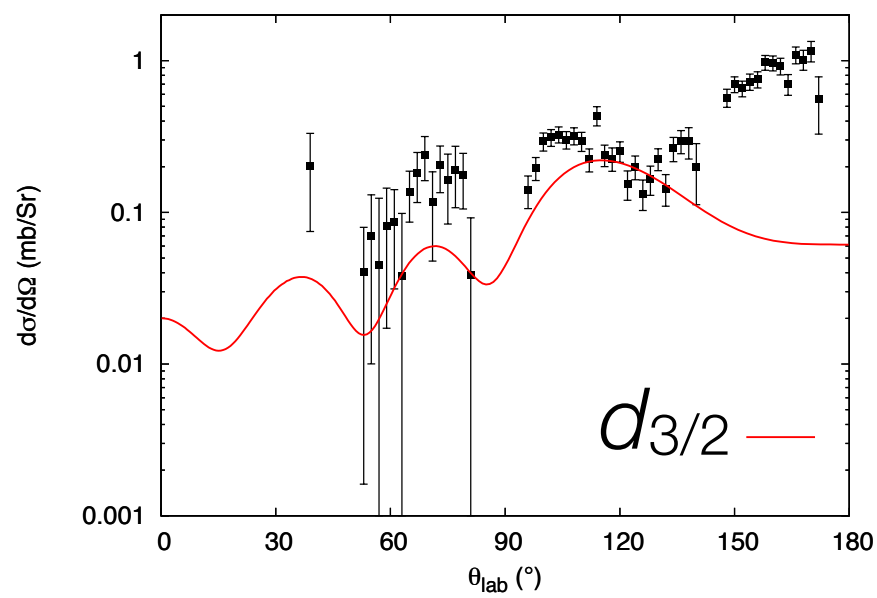
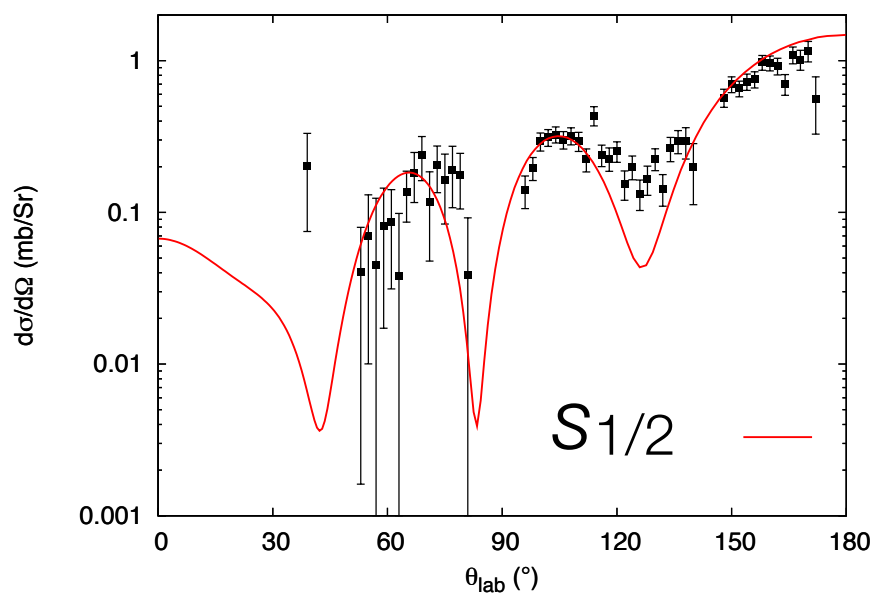
$^{26}\text{Na}$



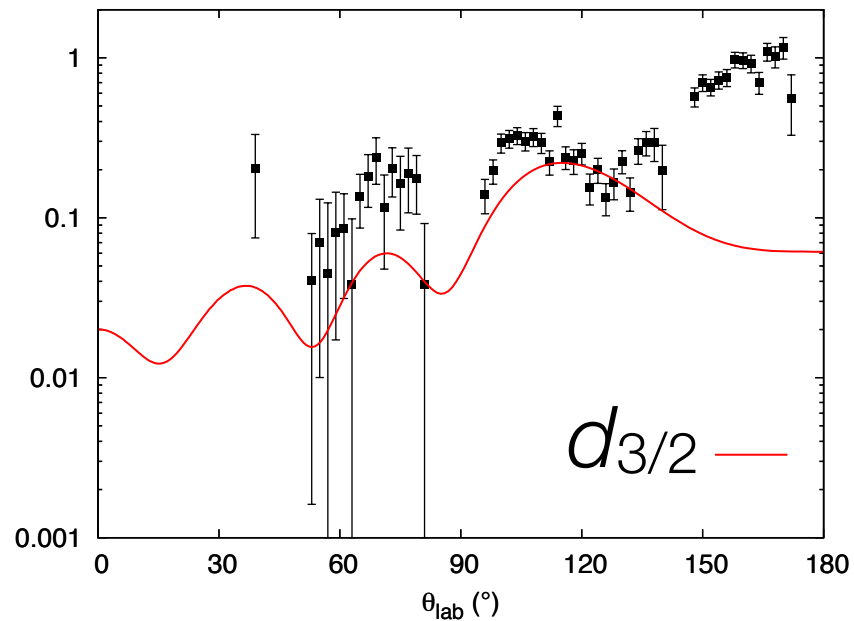
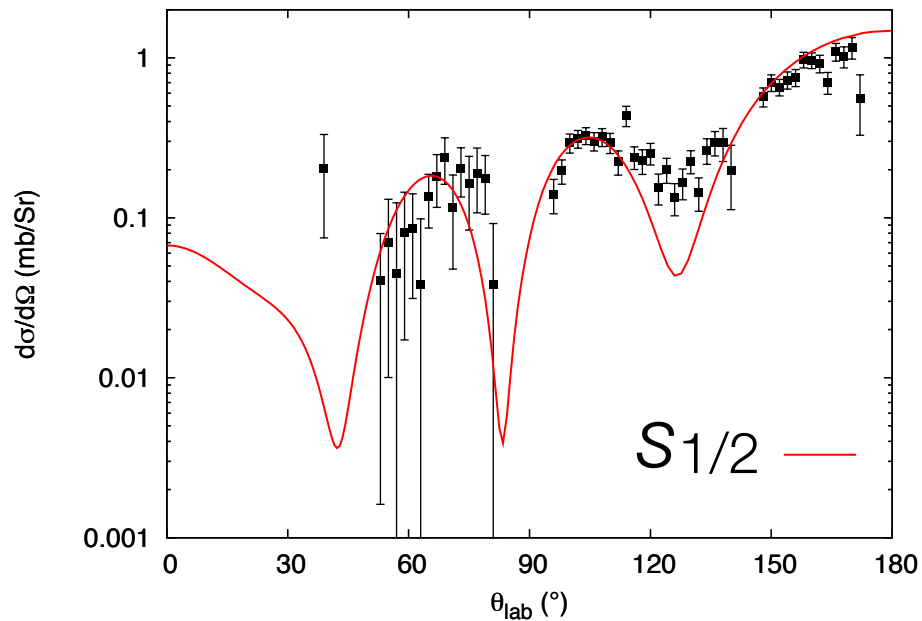
# Angular distributions

- 7 states in  $^{26}\text{Na}$  with a ground-state decay branch analysed
- Proton angular distributions extracted from  $\gamma$ -ray gating
- $\ell$ -transfer deduced from proton angular distributions
- Theoretical cross-sections calculated using ADWA Johnson-Soper method (R.C. Johnson and P.J.R. Soper, Phys. Rev. C. **1**, 976 (1970))
- For states with no angular distribution extracted,  $J^\pi$  assignments inferred from the N=15 isotone,  $^{28}\text{Al}$

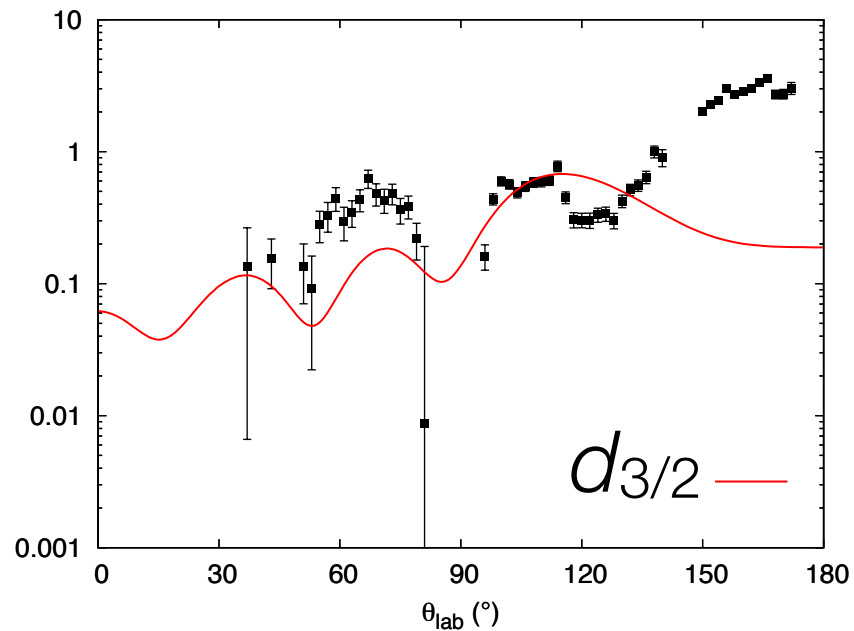
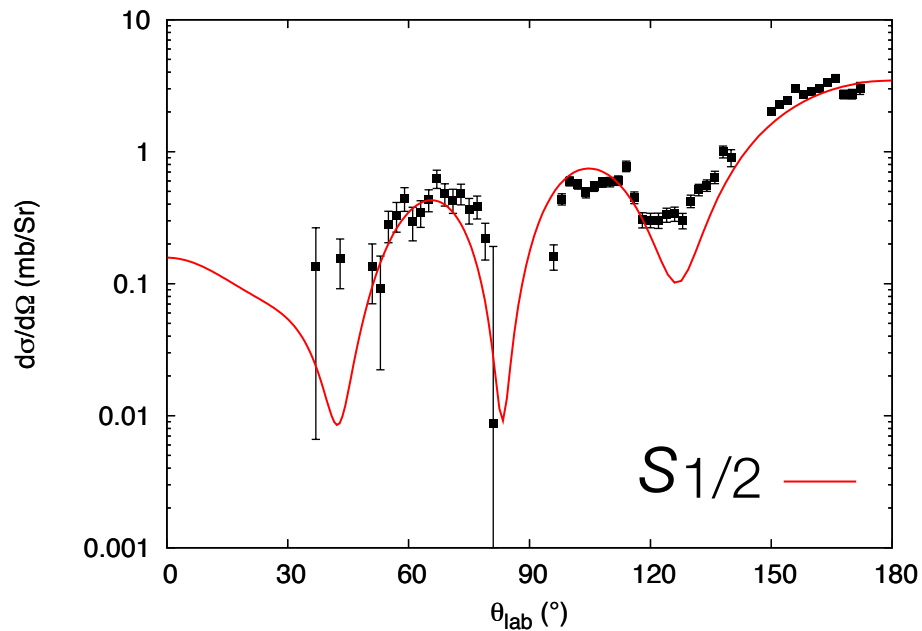
## 233-keV state:



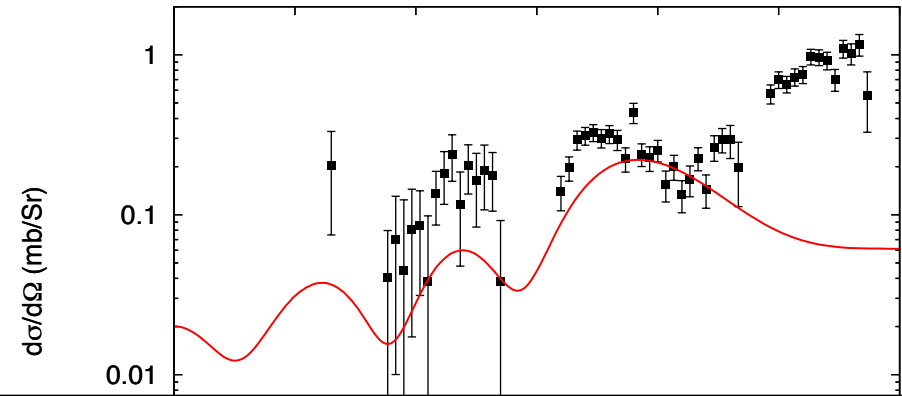
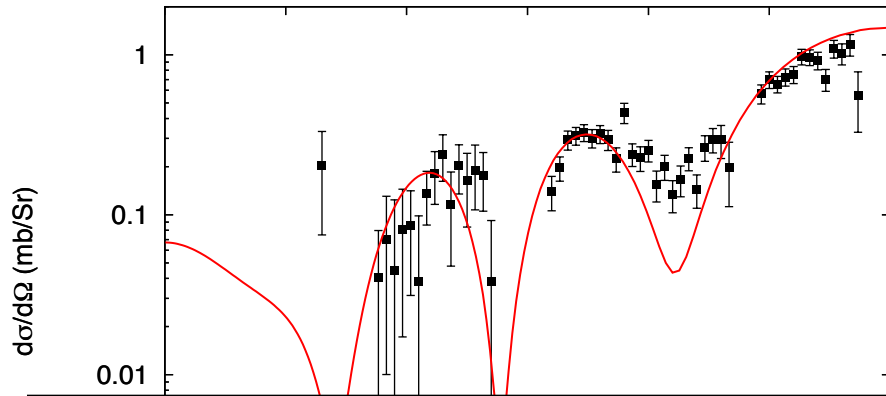
# 233-keV state:



# 407-keV state:



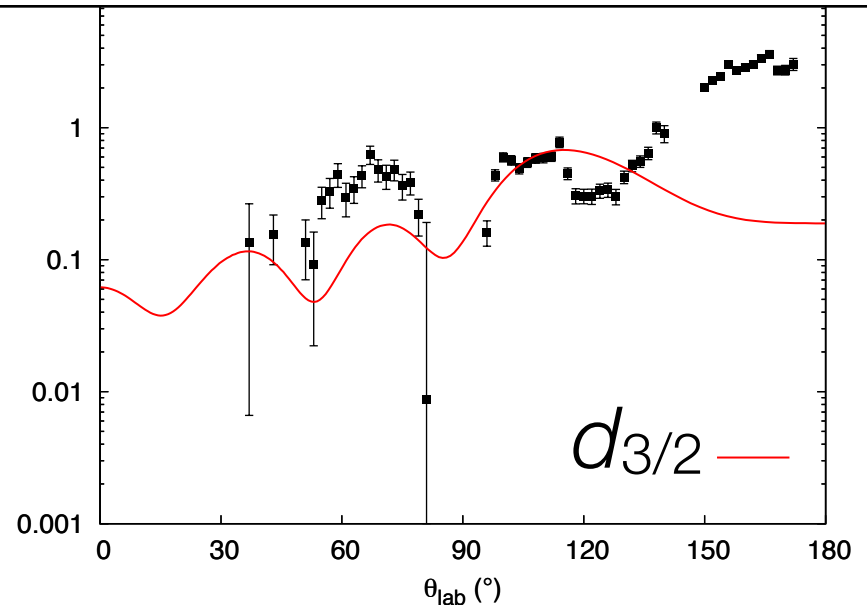
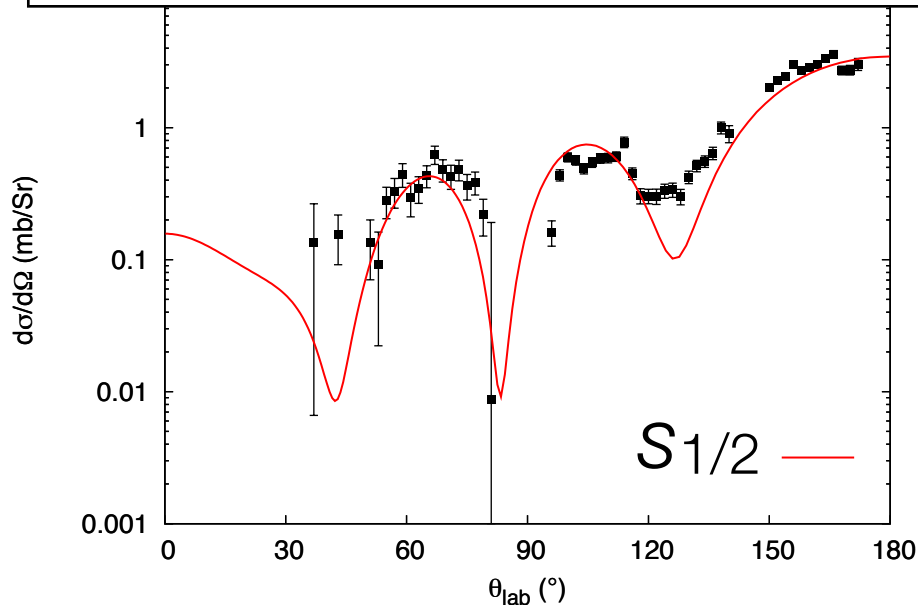
# 233-keV state:



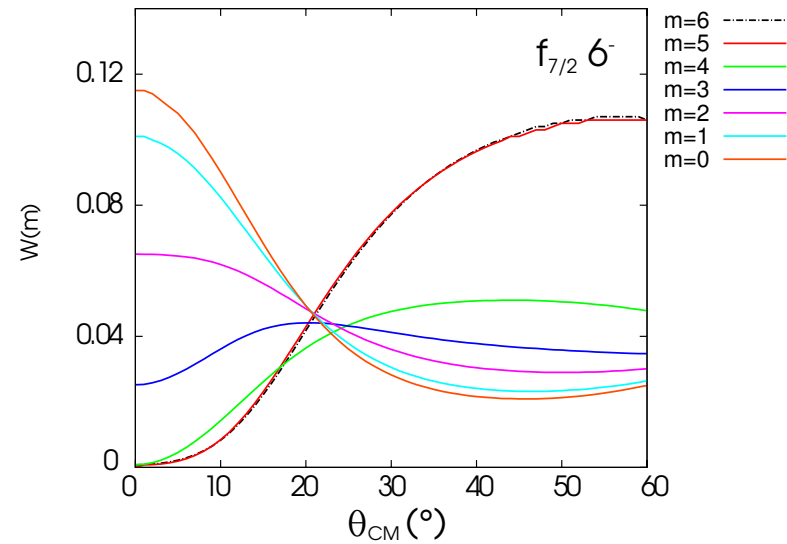
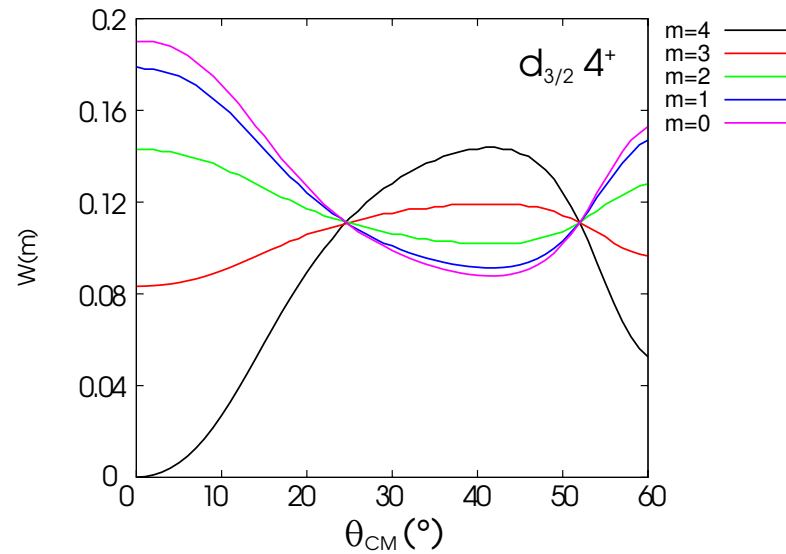
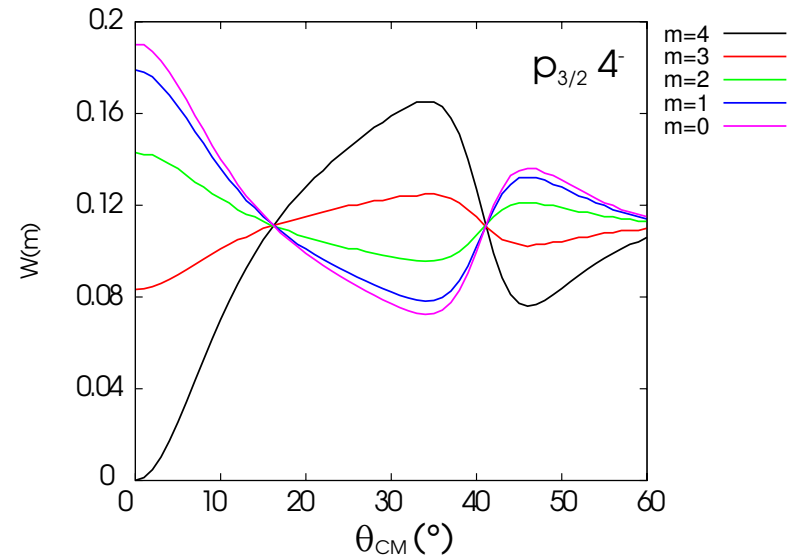
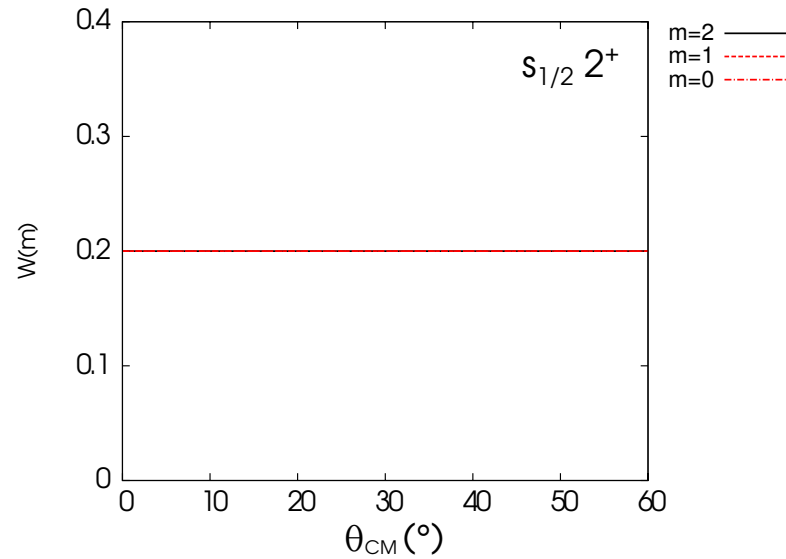
There have been no previous direct measurements of the 233- or 407-keV states; they have only been previously deduced to be  $2^+$  [1,2]

[1] Sangjin Lee *et al.*, Phys. Rev. C **73**, 044321 (2006) -  $^{14}\text{C}(^{14}\text{C},d)$

[2] K.I. Pearce *et al.*, Phys. Rev. C **35**, 5 (1987) -  $^{26}\text{Mg}(^3\text{H}, ^3\text{He})^{26}\text{Na}$



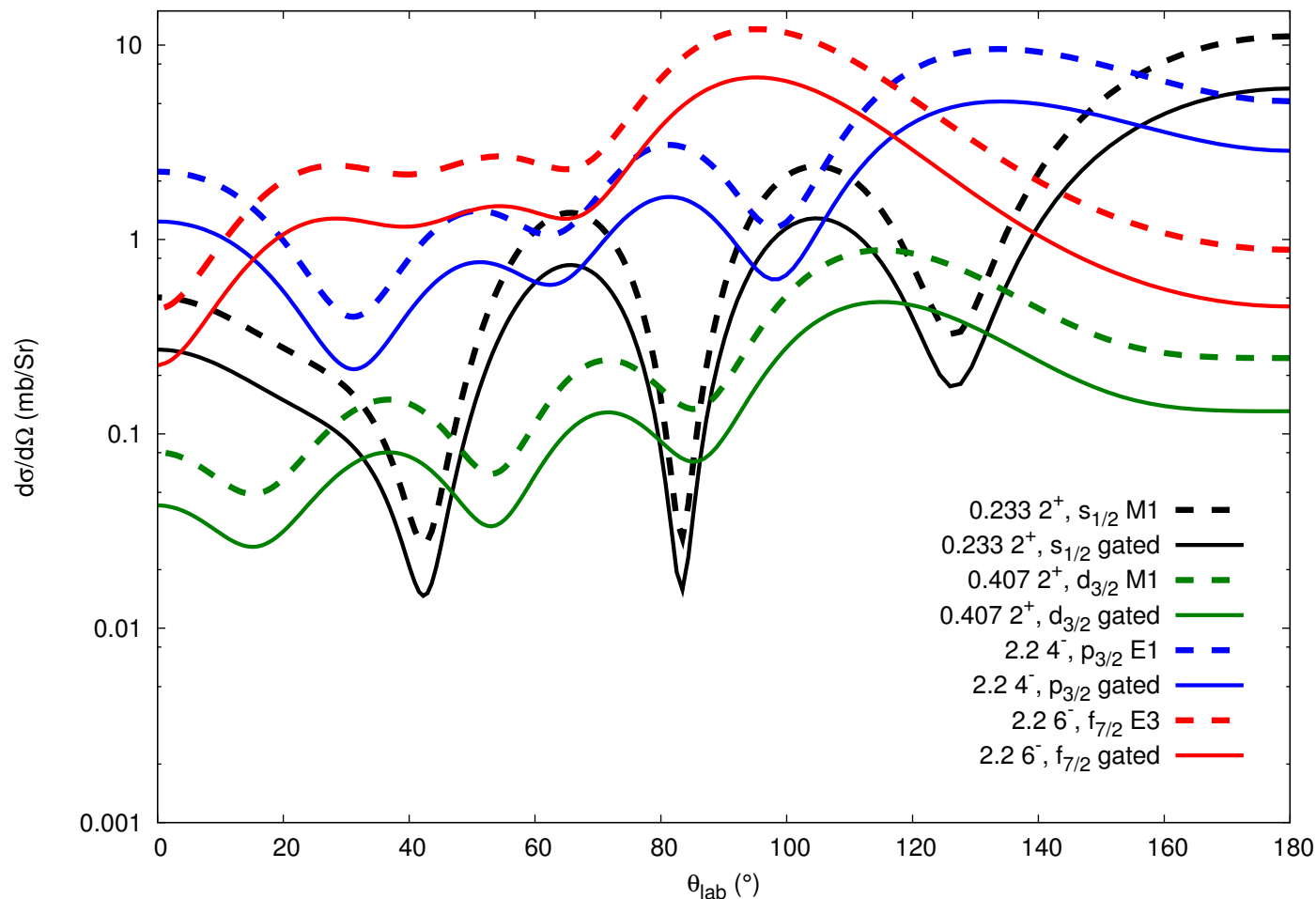
# Substate populations over proton CM angle for a 2.2 MeV state in $^{26}\text{Na}$



The  $\gamma$ -ray angular distribution varies as a function of proton angle, so proton angular distributions are distorted if extracted with the requirement of a  $\gamma$  ray. The effect is calculated by integrating the calculated  $\gamma$ -ray angular distribution for each proton angle over the range of the TIGRESS detectors.

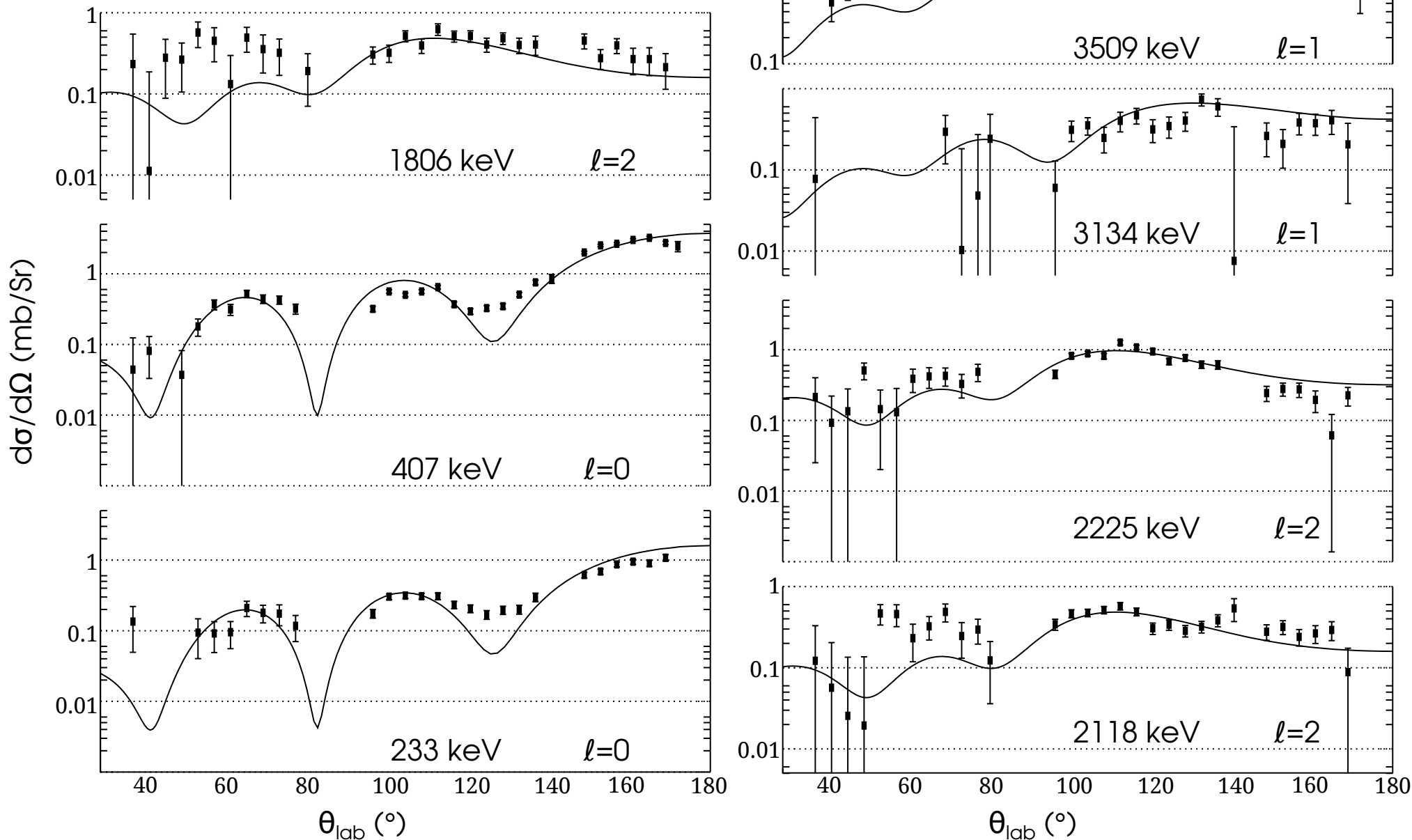


# Comparison of proton angular distributions with and without a $\gamma$ -ray gate



Gating does not affect the shape of the angular distribution, but the size of the cross section. The spectroscopic factor is recovered by correcting for the measured  $\gamma$ -ray efficiency.

# Proton angular distributions



Theoretical cross-sections calculated using TWOFNR, using the zero-range ADWA method[1].

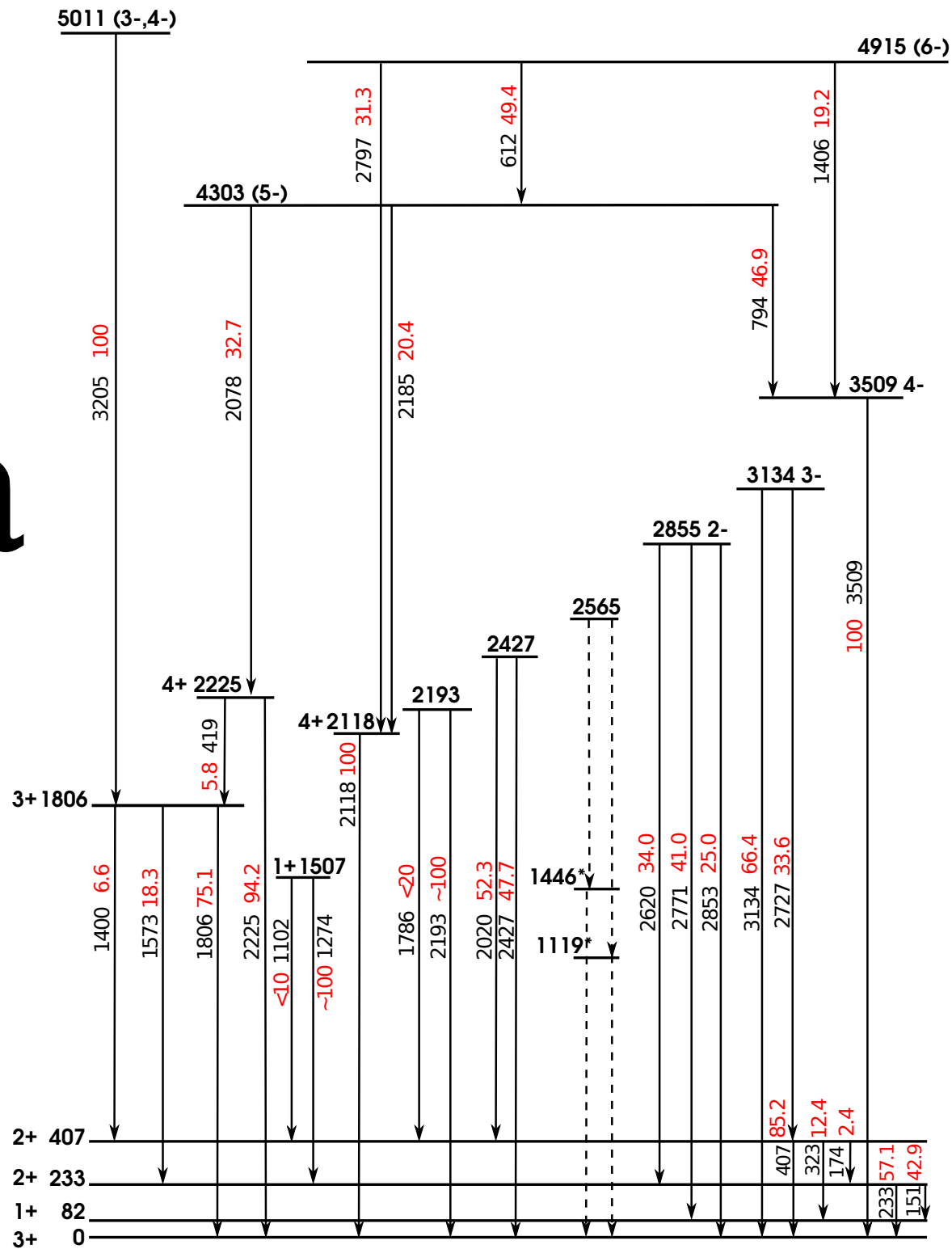
[1] R.C. Johnson and P.J.R. Soper, Phys. Rev. C **1**, 976 (1970)

# $^{26}\text{Na}$

This work

Energies in keV

Branching ratios  
in red

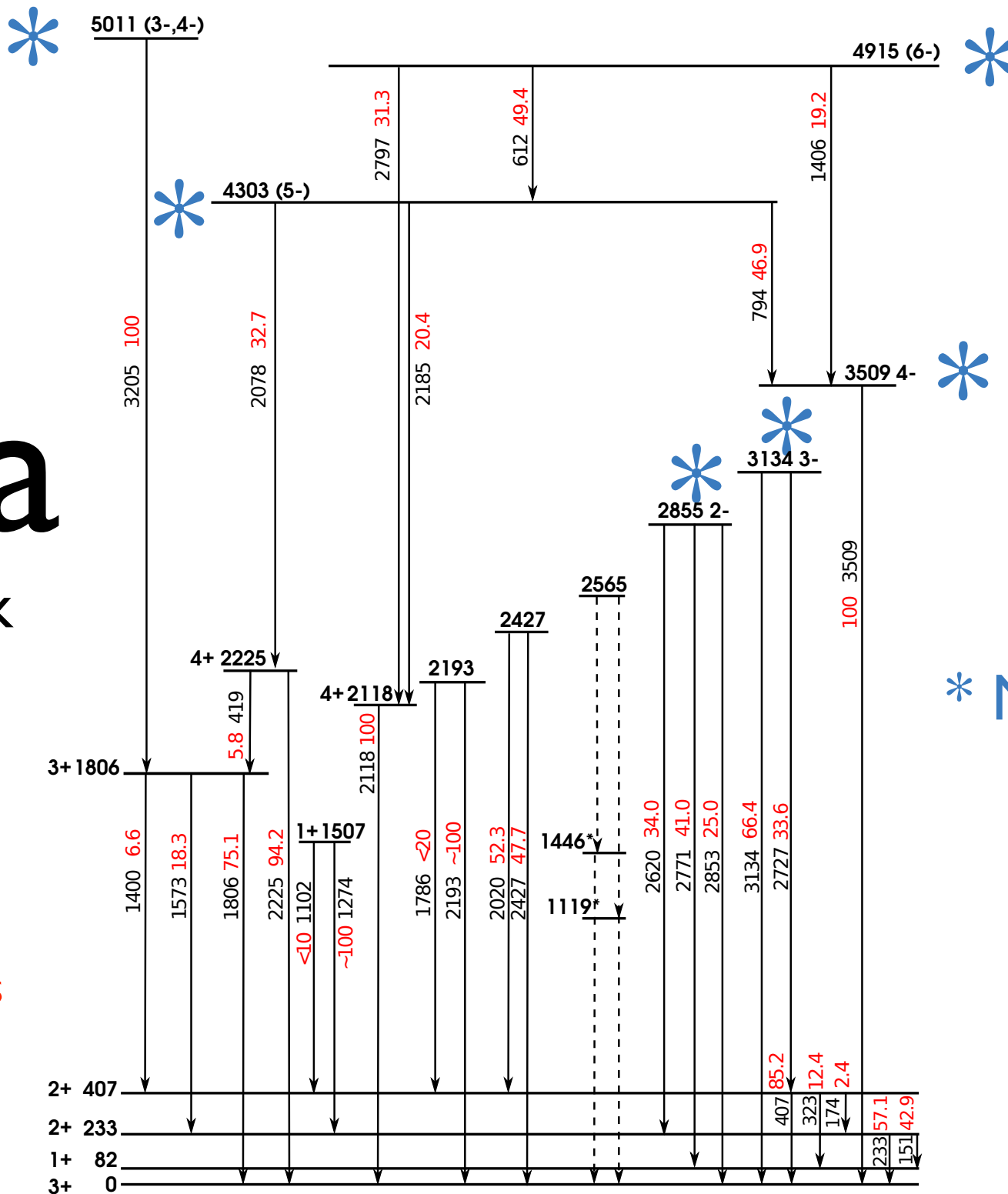


# $^{26}\text{Na}$

This work

Energies in keV

Branching ratios  
in red



\* Negative parity states

# Final Spectroscopic Factors

This work

*sdpf* model space with 0.7 MeV reduction  
between the *sd*- and *pf*-shells

$E^*$ (MeV)	coupling	S.F. $\pm$ ~20%	$J^\pi$	$E^*$ (MeV)	coupling	S.F. $\pm$ ~20%	$J^\pi$
3.512	$p_{3/2}$	0.54	$4^-$	3.613	$p_{3/2}$	0.43	$4^-$
3.136	$p_{3/2}$	0.10	$3^-$	3.377*	$p_{3/2}$	0.15	$3^-$
2.226	$d_{3/2}$	0.43	$4^+$	1.648	$d_{3/2}$	0.59	$4^+$
2.119	$d_{3/2}$	0.22	$4^+$				
1.807	$d_{3/2}$	0.22	$3^+$	1.247	$d_{3/2}$	0.32	$3^+$
0.407	$s_{1/2}$	0.34	$2^+$	0.231	$s_{1/2}$	0.19	$2^+$
0.233	$s_{1/2}$	0.14	$2^+$	0.05	$s_{1/2}$	0.22	$2^+$

\*This state also has an  $f_{7/2}$  component, S.F. = 0.17

# Findings - calculations

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- Identified key states in  $^{26}\text{Na}$  for comparison with the shell model. In this region, the shell model is having to reproduce negative-parity states at relatively low energies, and with the  $v(d_{3/2})$  orbital giving states lower than the  $7/2$ .
- SPDF-M calculations previously failed in this region ( $^{27}\text{Ne}$ ), which motivated WBP. WBP-M found good agreement for positive and negative parity levels, and it predicts the multiplet splitting for the proton-neutron coupling well. Spectroscopic factors are well produced. WBP-M also worked for  $^{25}\text{Ne}$ [1] and  $^{27}\text{Ne}$ [2] with a 0.7 MeV shift.
- Full  $1\hbar\omega$  *s-p-sd-pf* WBP-M calculations now being finalised for  $^{26}\text{Na}$ , as presented for  $^{27}\text{Ne}$ . We are finding that the SF comparisons are unaffected, and the shift of 0.7 MeV is appropriate again.
- Calculations also done for the isotone  $^{28}\text{Al}$ , and a shift was also needed.

The states identified in  $^{26}\text{Na}$  are key for shell-model comparisons

[1] W.N. Catford, et al. Phys. Rev. Lett. **104**, 192501 (2010)

[2] S.M. Brown, et al. Phys. Rev. C **85**, 011302 (2012)

# Findings - future work

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- Technique of gating on a  $\gamma$  ray to extract proton angular distributions works well. Subsequent analysis showing that large angular coverage for  $\gamma$  rays is proving to be effective at giving negligible distortion of the proton differential cross-sections.
- Future: Complete  $^{26}\text{Na}$  analysis with further SF analysis for cascade decays of states and to extract the weaker states. Extend to  $^{29}\text{Mg}$  (N=17) to measure SFs for lowest levels and identify further single-particle strength that is predicted to be found higher in energy (approved at TRIUMF)

# Collaborators

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G. Hackman, A.B. Garnsworthy, S.J. Williams, C. Pearson, R. Churchman, M. Djongolov, C. Unsworth and the TIGRESS collaboration

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F. Sarazin



C. Svensson

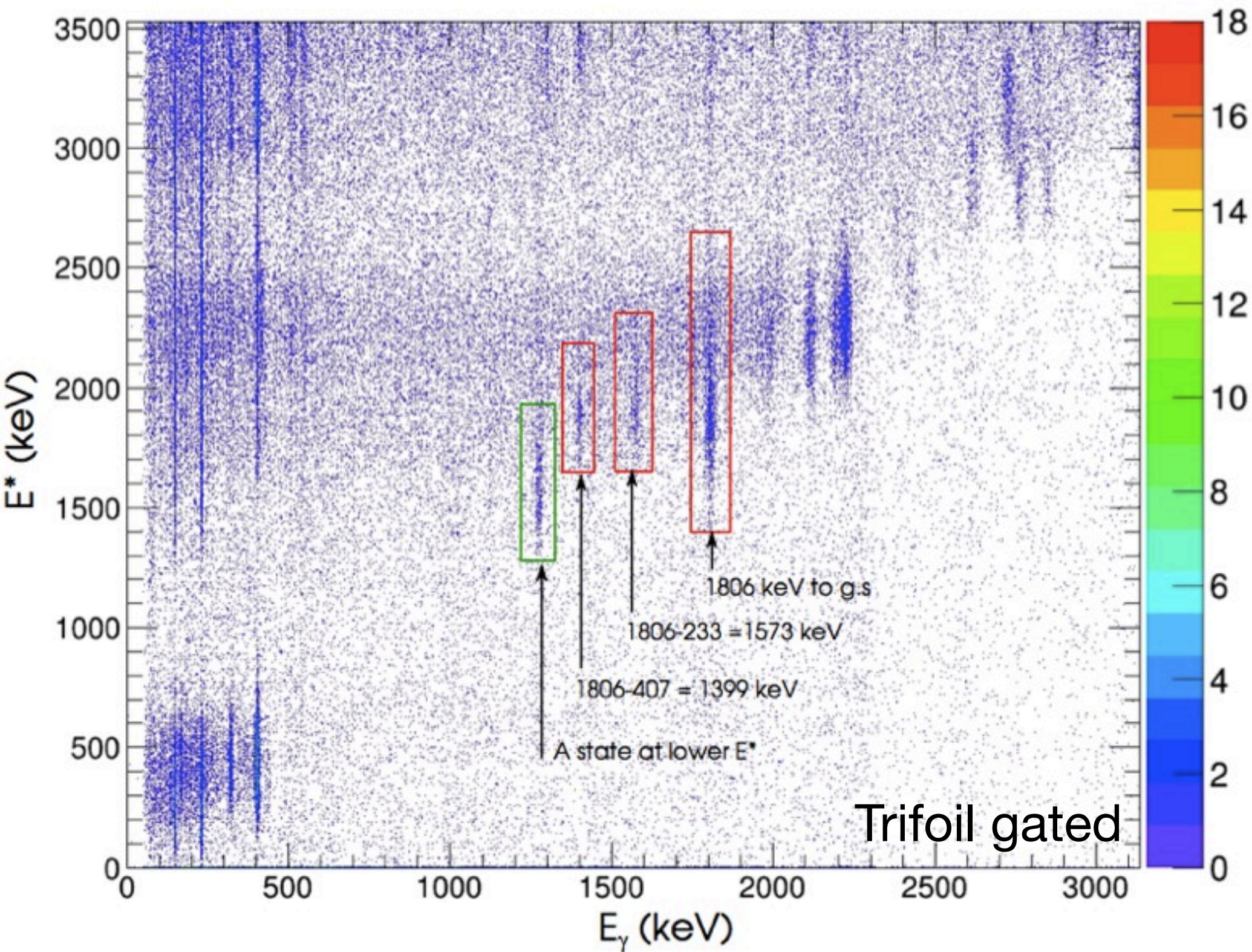


J.C. Blackmon



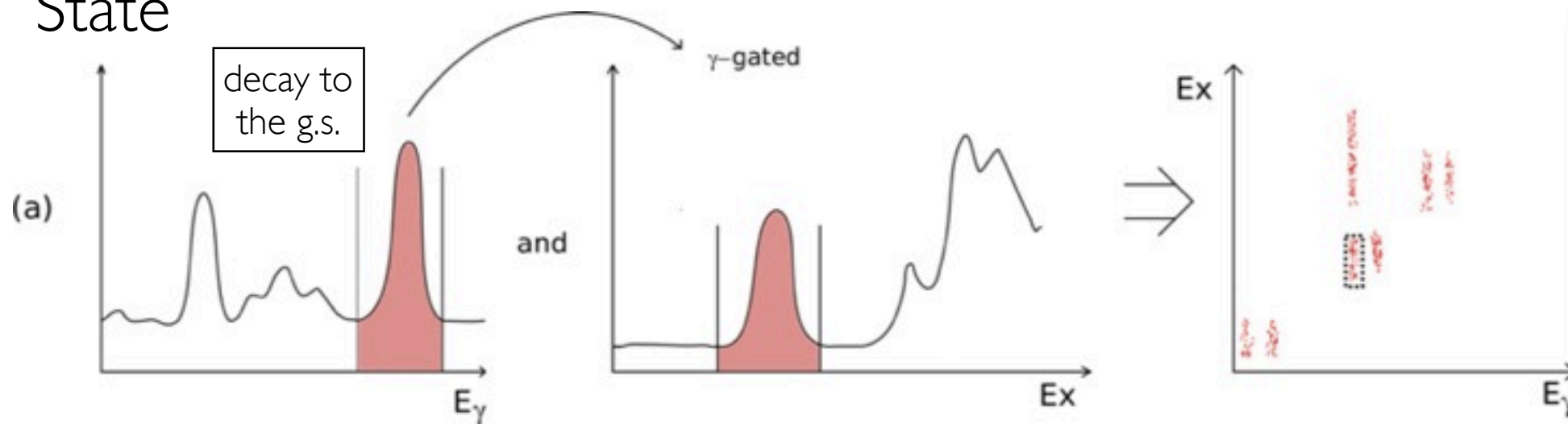
R.A.E. Austin



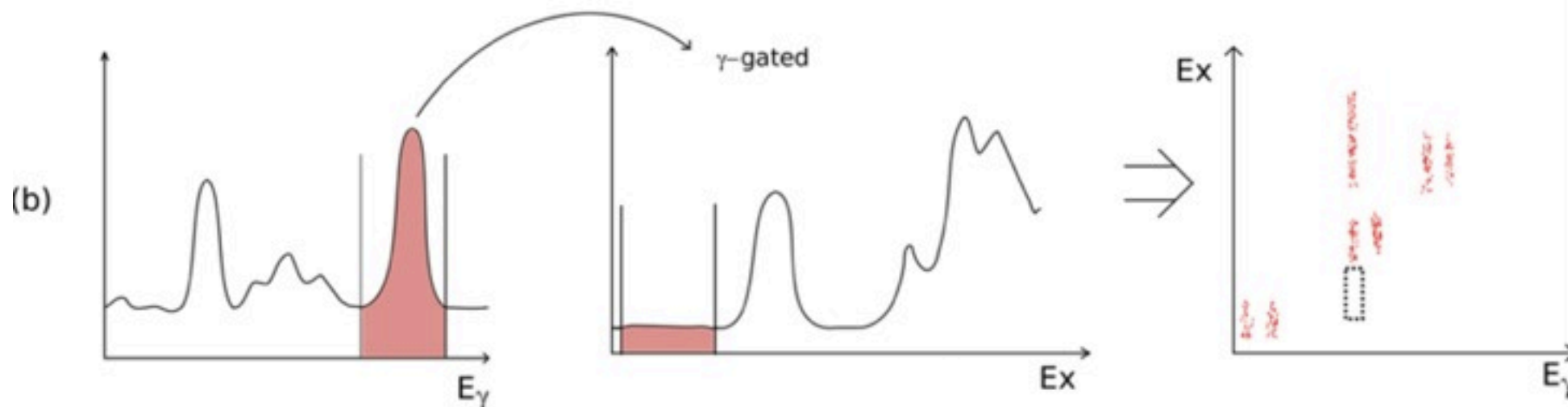


# Gating technique

## State



## Background - general case



# Findings

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The energies of the negative parity states in  $^{26}\text{Na}$  agree with predictions, to within  $\sim 100$  keV when the gap between the  $sd$ - and  $pf$ -shells was reduced by 0.7 MeV relative to WBP in the  $s$ - $p$ - $sd$ - $pf$  calculation

This systematic lowering of the shell gap was also applicable in the study of  $^{25}\text{Ne}$ [1] and  $^{27}\text{Ne}$ [2]

As previously seen in  $^{25}\text{Ne}$  [1], we see the  $\mathbf{v}(d_{3/2})$  states  $\sim 0.5$  MeV higher than predicted than WBP (which uses USD in the  $sd$ -shell)

These findings should motivate improvements to the shell model interactions to remove the need for ad hoc adjustments of single particle levels

[1] W.N. Catford, *et al.* Phys. Rev. Lett. **104**, 192501 (2010)

[2] S.M. Brown, *et al.* Phys. Rev. C **85**, 011302 (2012)