



Carlo Barbieri — University of Surrey

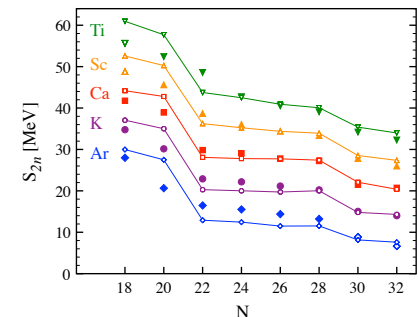
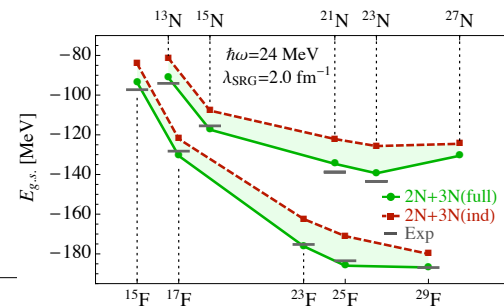
# Three-Nucleon Forces in Neutron Rich Isotopes (from O to Ni)

Collaborators:

A. Cipollone, CB, P. Navrátil:

*Phys. Rev. Lett.* **111**, 062501 (2013)

V. Somà, A. Cipollone, CB, P. Navrátil, T. Duguet: *Phys. Rev. C* **89**, 061301R (2014)



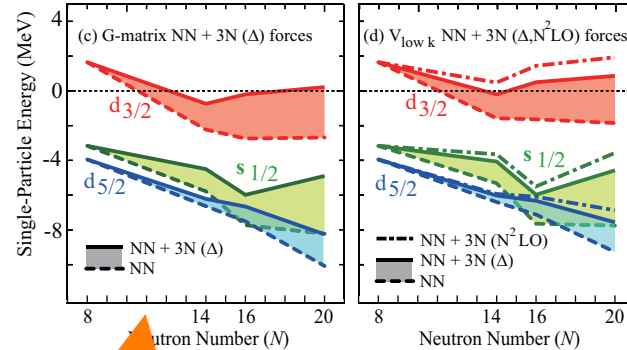
# Modern realistic nuclear forces

## Chiral EFT for nuclear forces:

	2N forces	3N forces	4N forces
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N <sup>2</sup> LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N <sup>3</sup> LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

(3NFs arise naturally at N2LO)

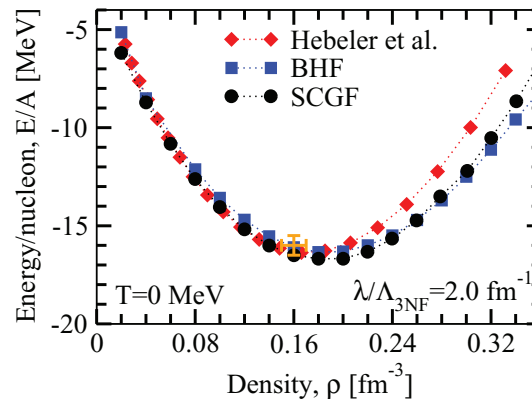
## Single particle spectrum at $E_{\text{fermi}}$ :



[T. Otsuka et al., Phys Rev. Lett **105**, 032501 (2010)]

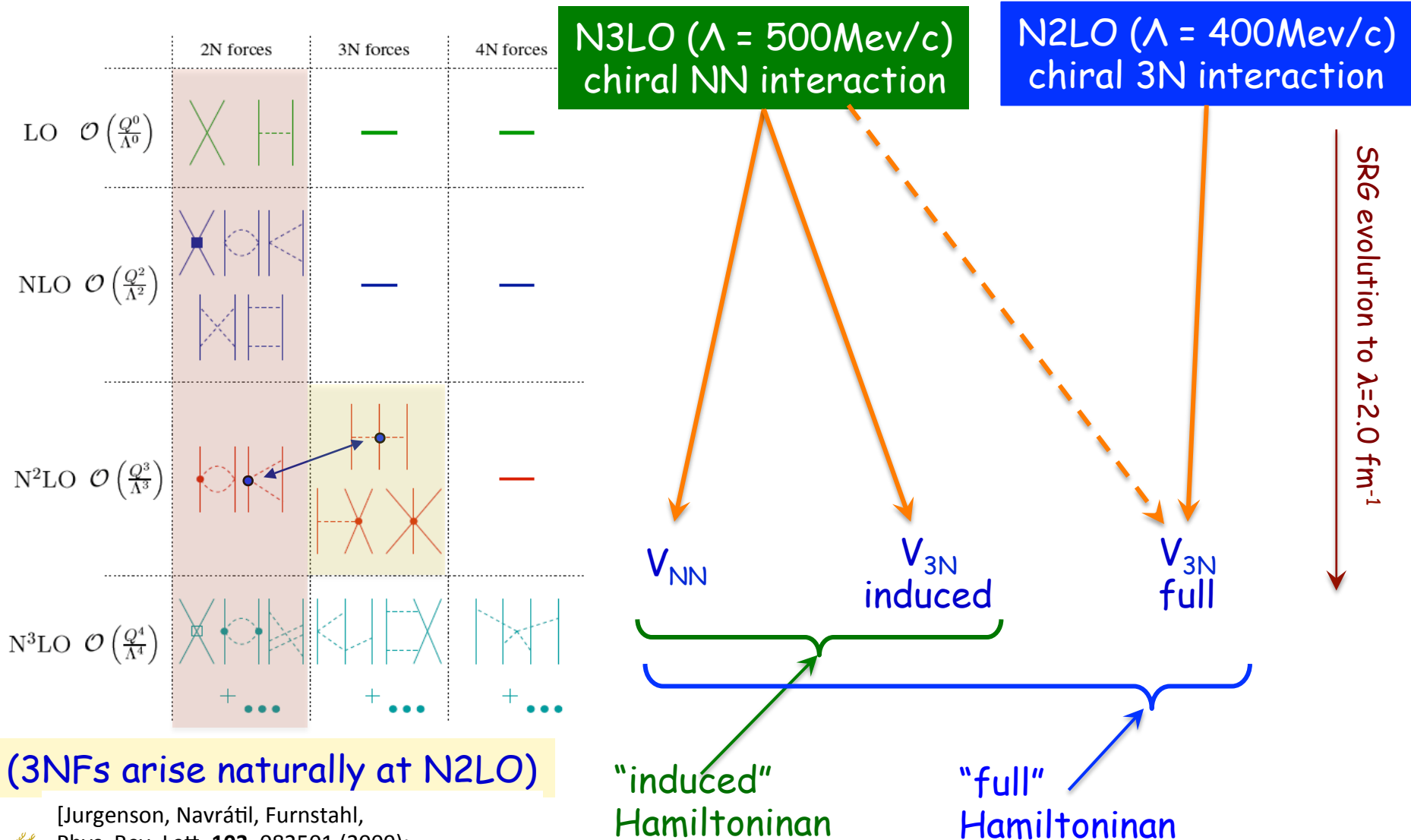
Need at LEAST 3NF!!!  
("cannot" do RNB physics without...)

## Saturation of nuclear matter:



[A. Carbone et al., Phys Rev. C **88**, 044302 (2013)]

# Chiral Nuclear forces - SRG evolved



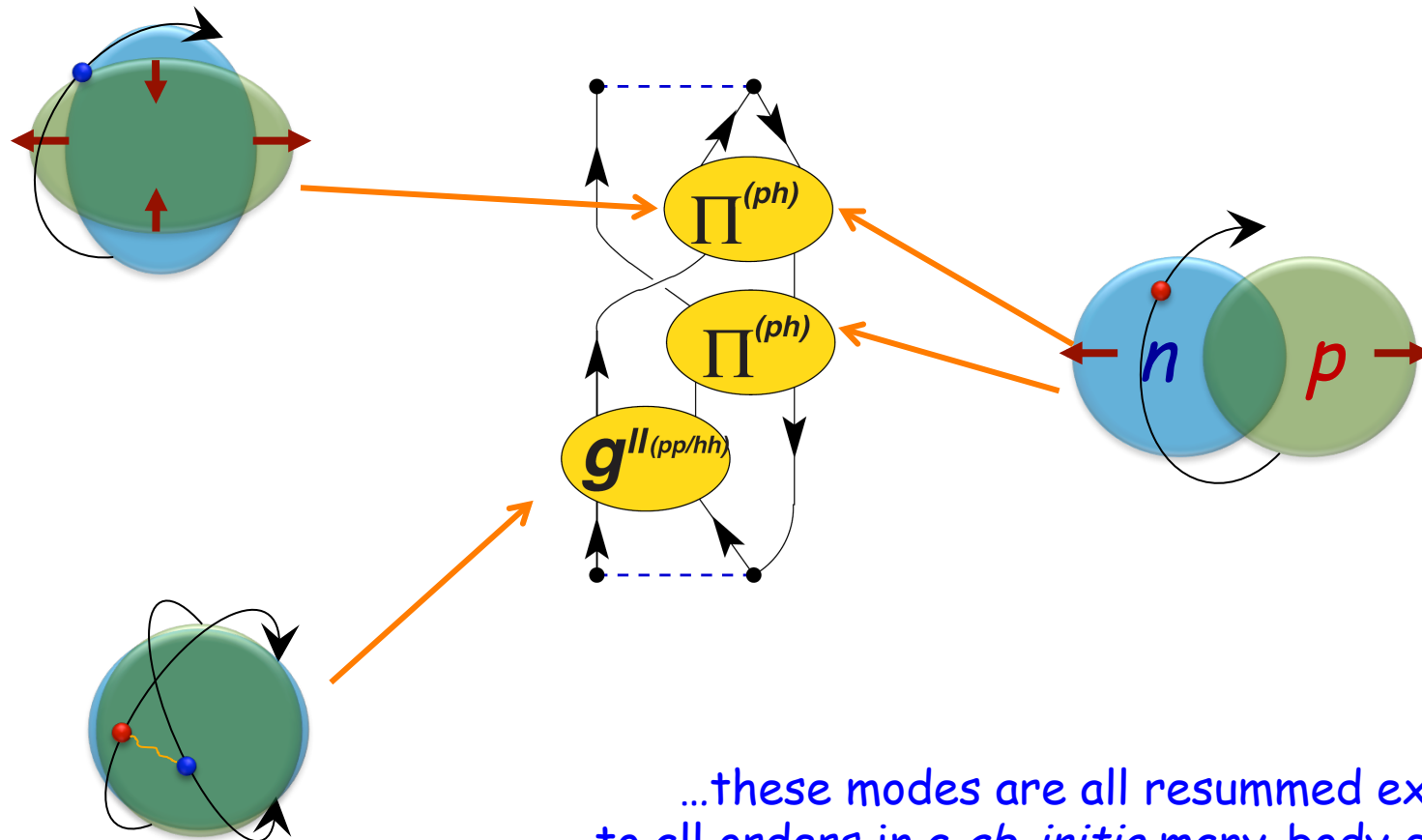
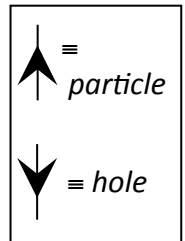
(3NFs arise naturally at N2LO)

[Jurgenson, Navrátil, Furnstahl,  
Phys. Rev. Lett. **103**, 082501 (2009);  
Hebeler, Phys. Rev. C **85**, 021002 (2012)]



# Faddeev-RPA in two words...

Particle vibration coupling is the main cause driving the distribution of particle strength—a least close to the Fermi surface...



...these modes are all resummed exactly and to all orders in a *ab-initio* many-body expansion.

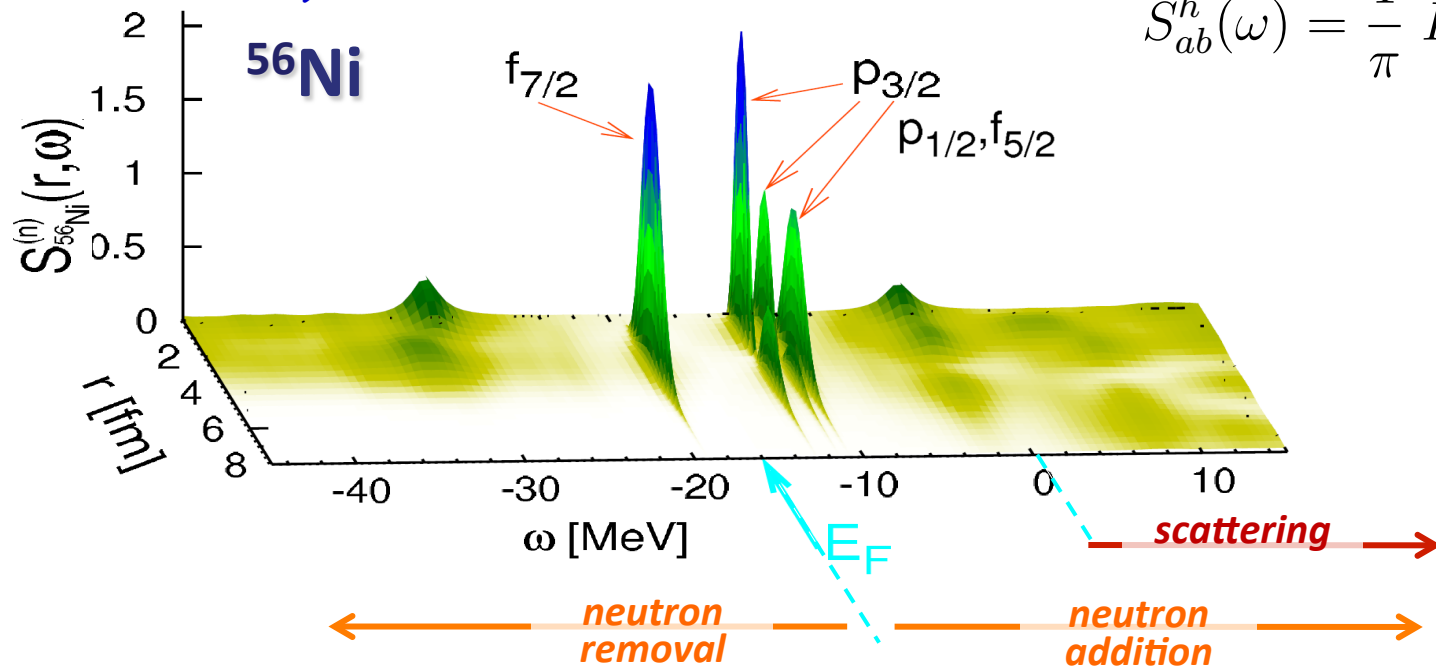
# Green's functions in many-body theory

One-body Green's function (or propagator) describes the motion of quasi-particles and holes:

$$g_{\alpha\beta}(E) = \sum_n \frac{\langle \Psi_0^A | c_\alpha | \Psi_n^{A+1} \rangle \langle \Psi_n^{A+1} | c_\beta^\dagger | \Psi_0^A \rangle}{E - (E_n^{A+1} - E_0^A) + i\eta} + \sum_k \frac{\langle \Psi_0^A | c_\beta^\dagger | \Psi_k^{A-1} \rangle \langle \Psi_k^{A-1} | c_\alpha | \Psi_0^A \rangle}{E - (E_0^A - E_k^{A-1}) - i\eta}$$

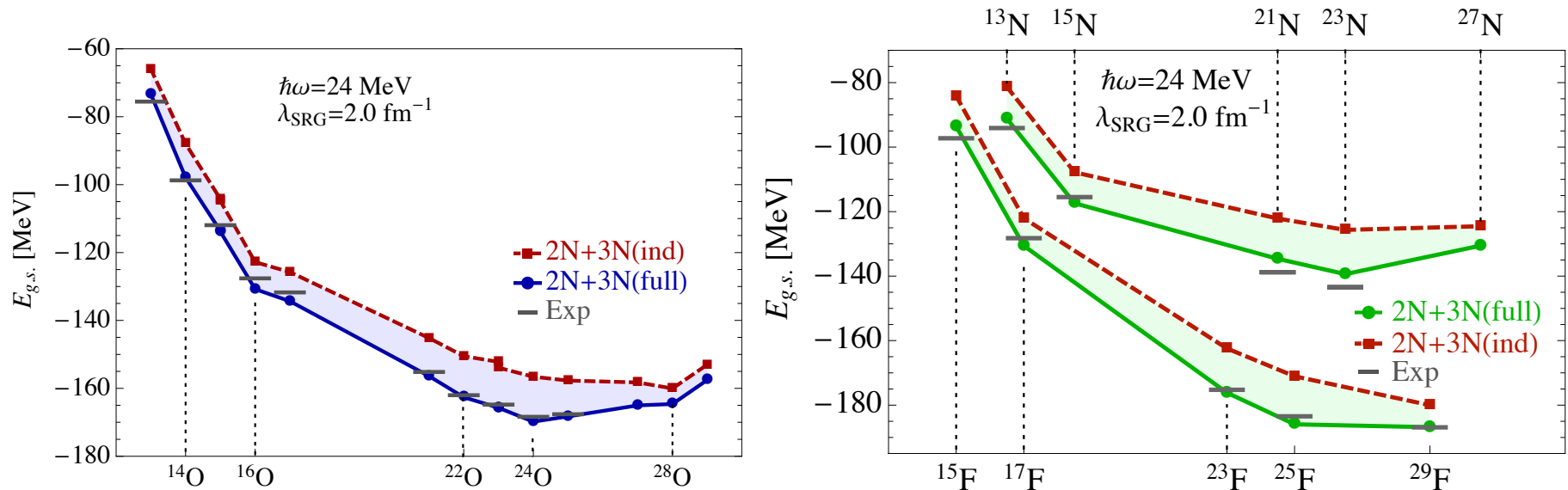
...this *contains all the structure information* probed by nucleon transfer (spectral function):

$$S_{ab}^h(\omega) = \frac{1}{\pi} \text{Im} g_{ab}(\omega)$$



# Results for the N-O-F chains

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)



→ 3NF crucial for reproducing binding energies and driplines around oxygen

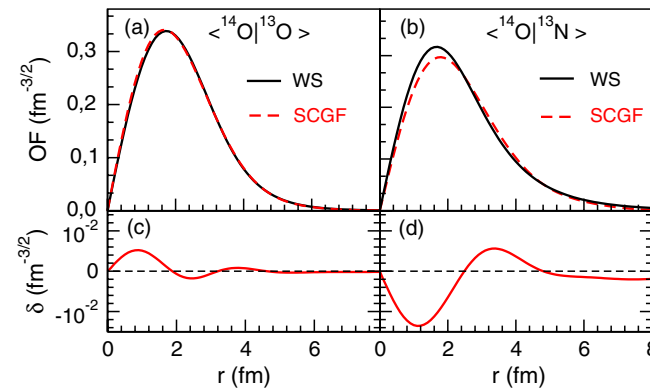
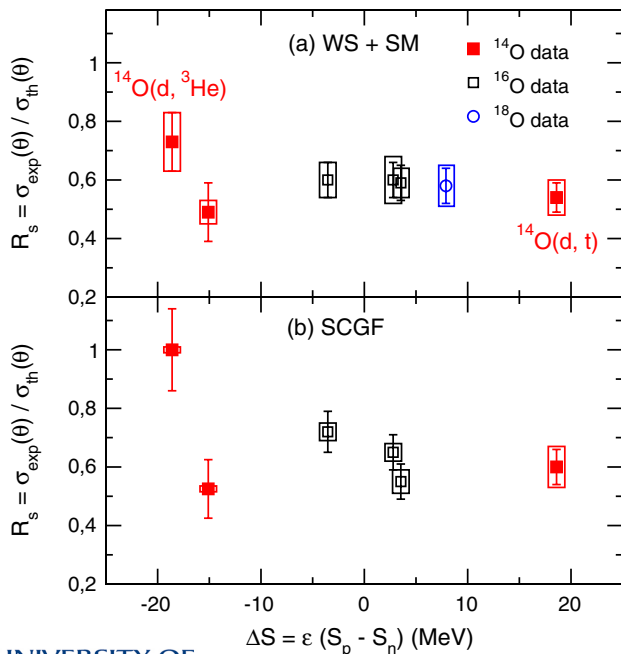
→ cf. microscopic shell model [Otsuka et al, PRL**105**, 032501 (2010).]

# Single nucleon transfer in the oxygen chain

[F. Flavigny et al, PRL110, 122503 (2013)]

→ Analysis of  $^{14}\text{O}(d,t)^{13}\text{O}$  and  $^{14}\text{O}(d,^3\text{He})^{13}\text{N}$  transfer reactions @ SPIRAL

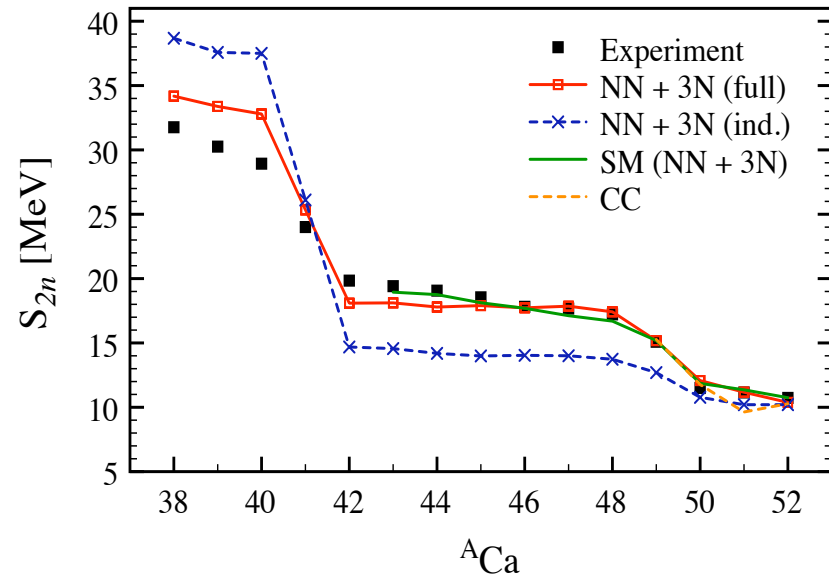
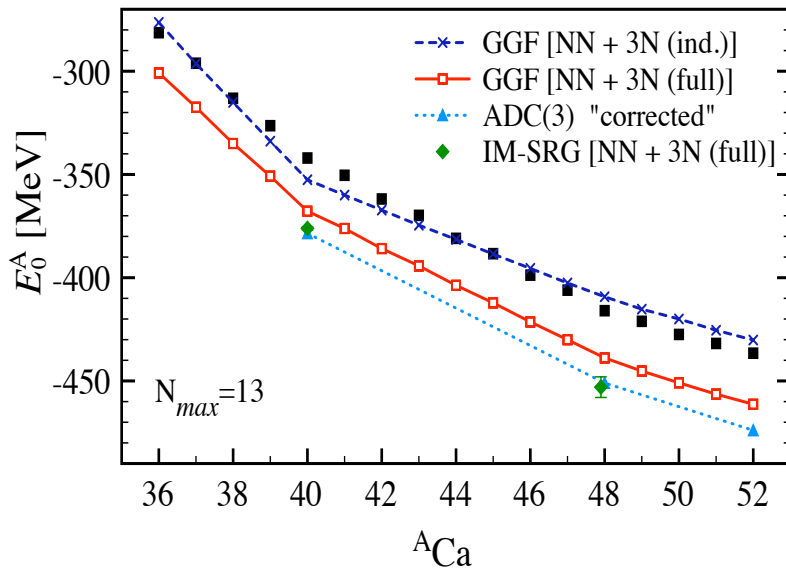
Reaction	$E^*$ (MeV)	$J^\pi$	$R_{\text{rms}}^{\text{HF}}^{\text{B}}$ (fm)	$r_0$ (fm)	$C^2S_{\text{exp}}$ (WS)	$C^2S_{\text{th}}$ $0p + 2\hbar\omega$	$R_s$ (WS)	$C^2S_{\text{exp}}$ (SCGF)	$C^2S_{\text{th}}$ (SCGF)	$R_s$ (SCGF)
$^{14}\text{O}(d,t)^{13}\text{O}$	0.00	$3/2^-$	2.69	1.40	1.69 (17)(20)	3.15	0.54(5)(6)	1.89(19)(22)	3.17	0.60(6)(7)
$^{14}\text{O}(d,^3\text{He})^{13}\text{N}$	0.00	$1/2^-$	3.03	1.23	1.14(16)(15)	1.55	0.73(10)(10)	1.58(22)(2)	1.58	1.00(14)(1)
	3.50	$3/2^-$	2.77	1.12	0.94(19)(7)	1.90	0.49(10)(4)	1.00(20)(1)	1.90	0.53(10)(1)
$^{16}\text{O}(d,t)^{15}\text{O}$	0.00	$1/2^-$	2.91	1.46	0.91(9)(8)	1.54	0.59(6)(5)	0.96(10)(7)	1.73	0.55(6)(4)
$^{16}\text{O}(d,^3\text{He})^{15}\text{N}$ [19,20]	0.00	$1/2^-$	2.95	1.46	0.93(9)(9)	1.54	0.60(6)(6)	1.25(12)(5)	1.74	0.72(7)(3)
	6.32	$3/2^-$	2.80	1.31	1.83(18)(24)	3.07	0.60(6)(8)	2.24(22)(10)	3.45	0.65(6)(3)
$^{18}\text{O}(d,^3\text{He})^{17}\text{N}$ [21]	0.00	$1/2^-$	2.91	1.46	0.92(9)(12)	1.58	0.58(6)(10)			



- Overlap functions and strengths from GF
- $R_s$  independent of asymmetry

# Calcium isotopic chain

Ab-initio calculation of the whole Ca: *induced* and *full3NF* investigated



→ *induced* and *full3NF* investigated

→ *genuine* (N2LO) 3NF needed to reproduce the energy curvature and  $S_{2n}$

→ N=20 and Z=20 gaps *overestimated!*

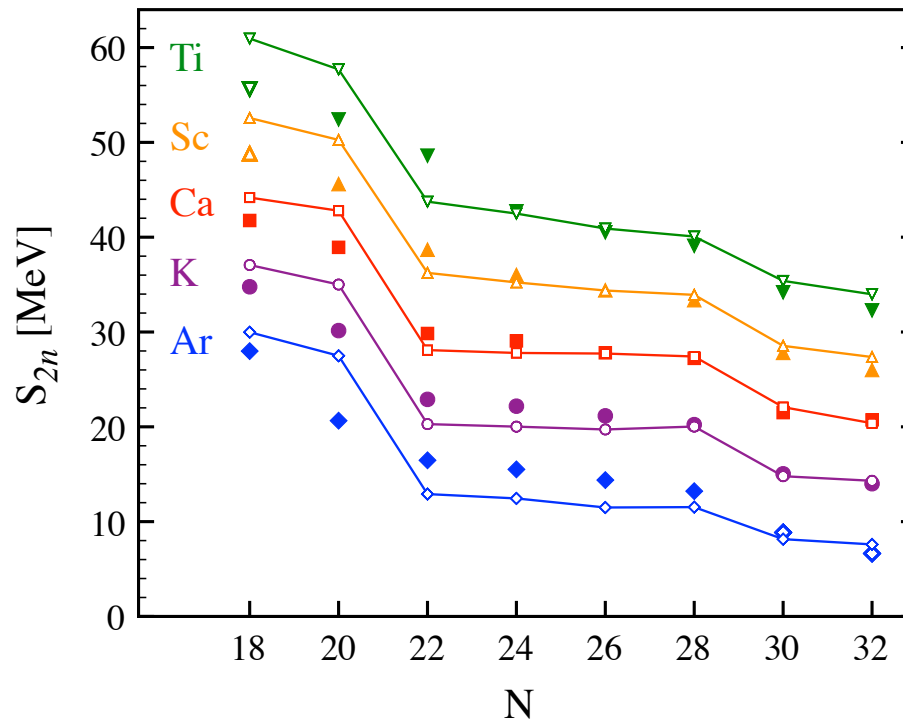
→ Full 3NF give a *correct trend* but *over bind!*



# Neighbouring Ar, K, Ca, Sc, and Ti chains

V. Somà, CB *et al.* Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:

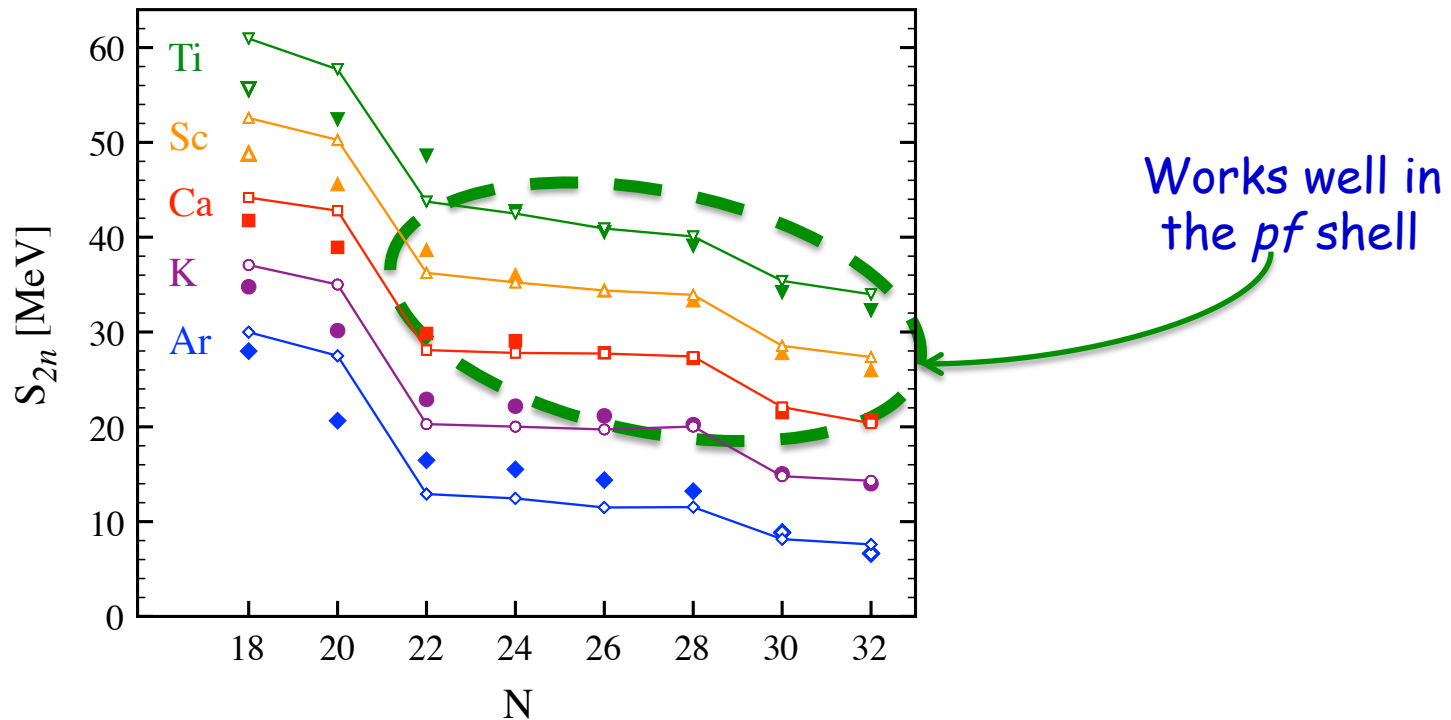


→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

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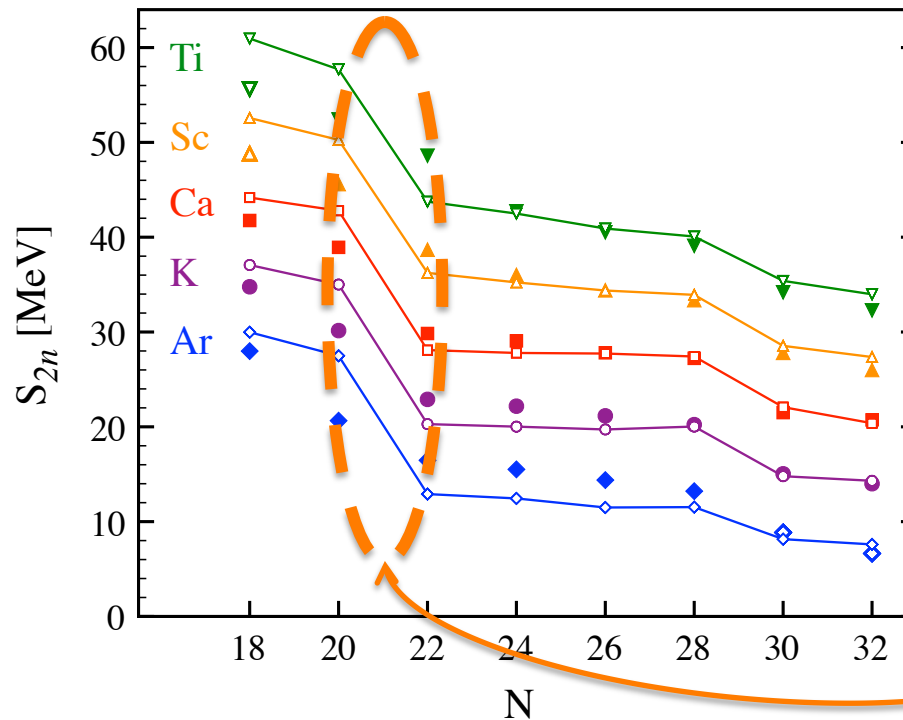


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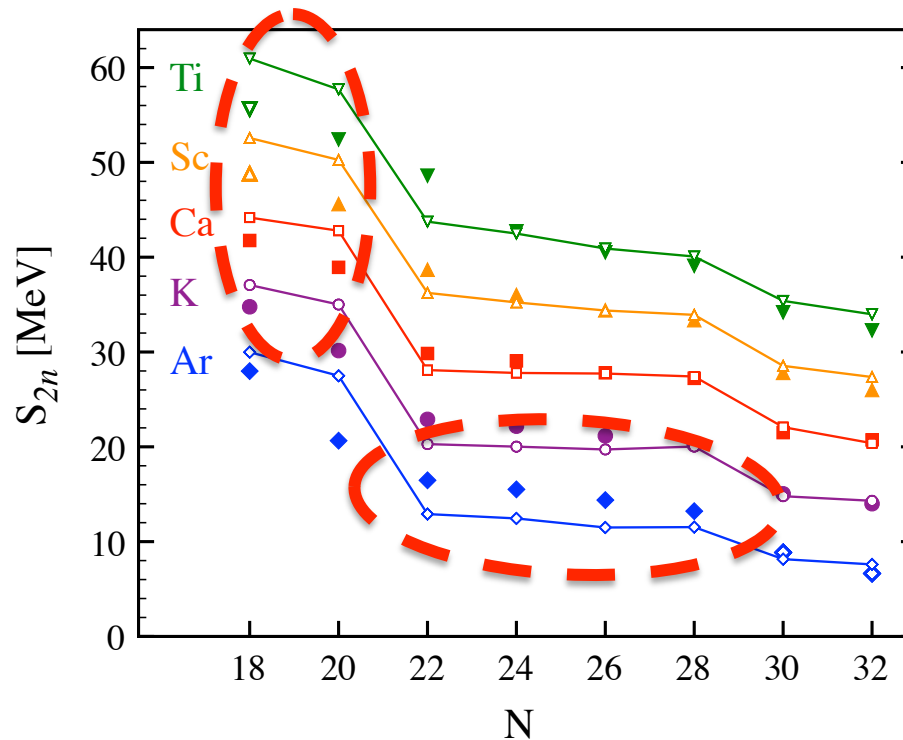
Over estimated  
N=20 and Z=20 gaps

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# Neighbouring Ar, K, Ca, Sc, and Ti chains

V. Somà, CB *et al.* Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:



Lack of deformation due to quenched cross-shell quadrupole excitations

→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

# Inversion of $d_{3/2}-s_{1/2}$ at $N=28$

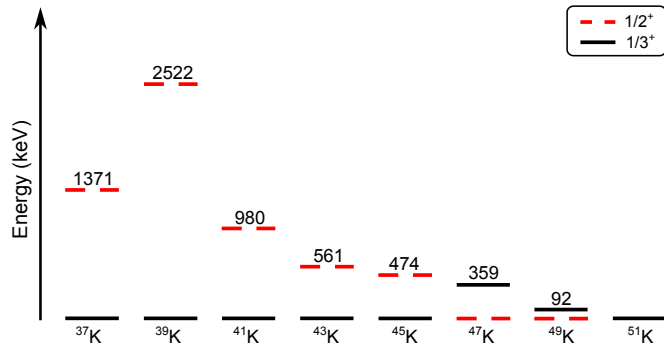
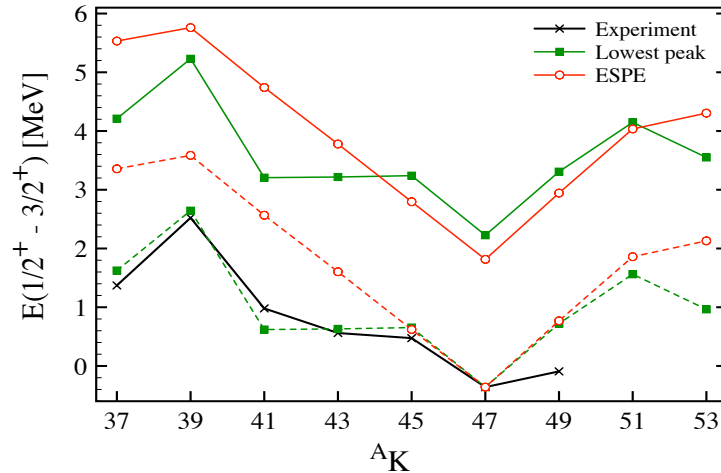
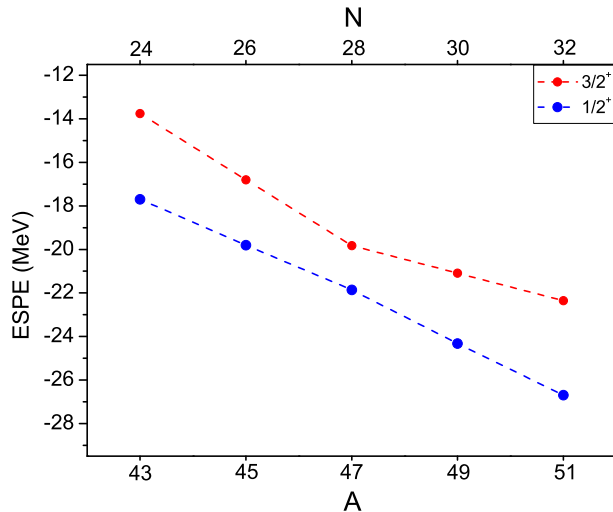


FIG. 1. (color online) Experimental energies for  $1/2^+$  and  $3/2^+$  states in odd-K isotopes. Inversion of the nuclear spin is obtained in  $^{47,49}\text{K}$  and reinversion back in  $^{51}\text{K}$ . Results are J. Papuga, et al., PRL **110**, 172503 (2013)

$A\text{K}$  isotopes  
Laser spectroscopy @ ISOLDE

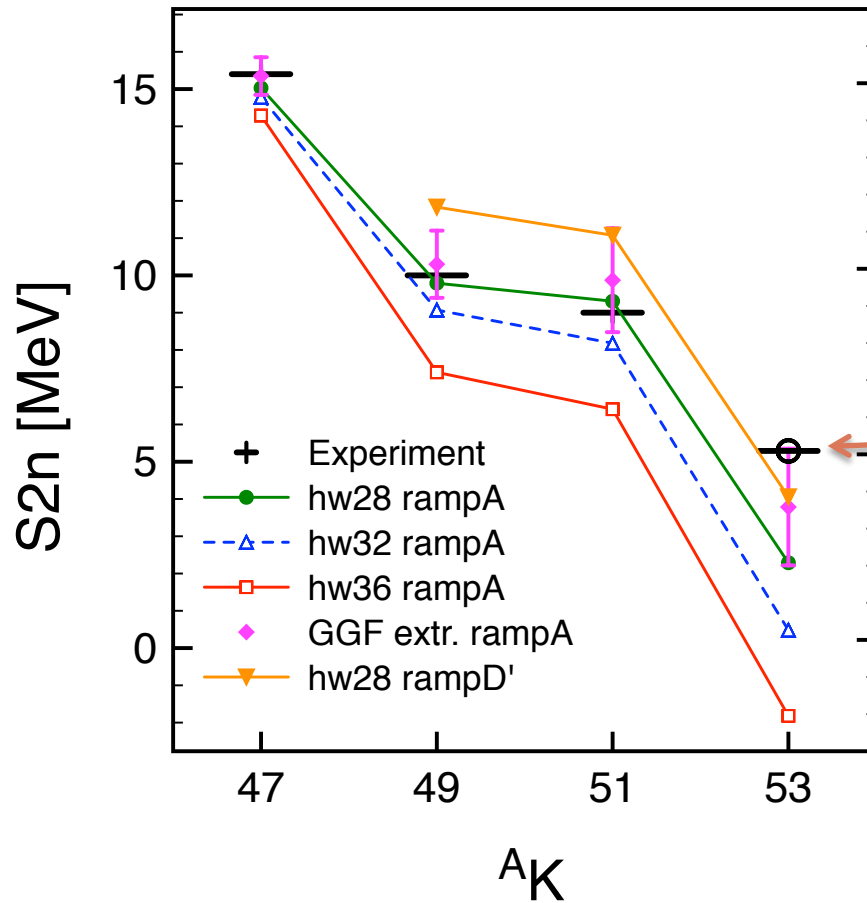
Change in separation described by chiral NN+3NF:



ESPE: "centroid" energies

(Gorkov calculations at 2<sup>nd</sup> order)

# Two-neutron separation energies for neutron rich K isotopes

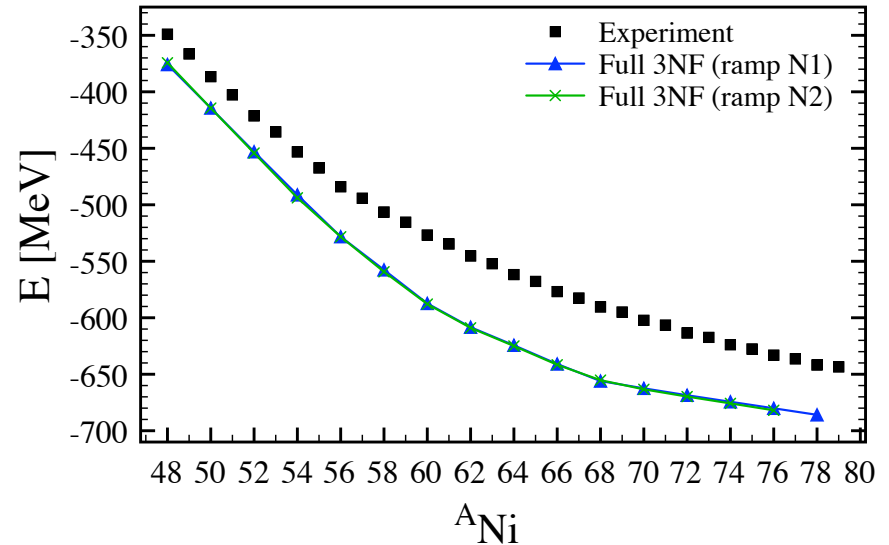
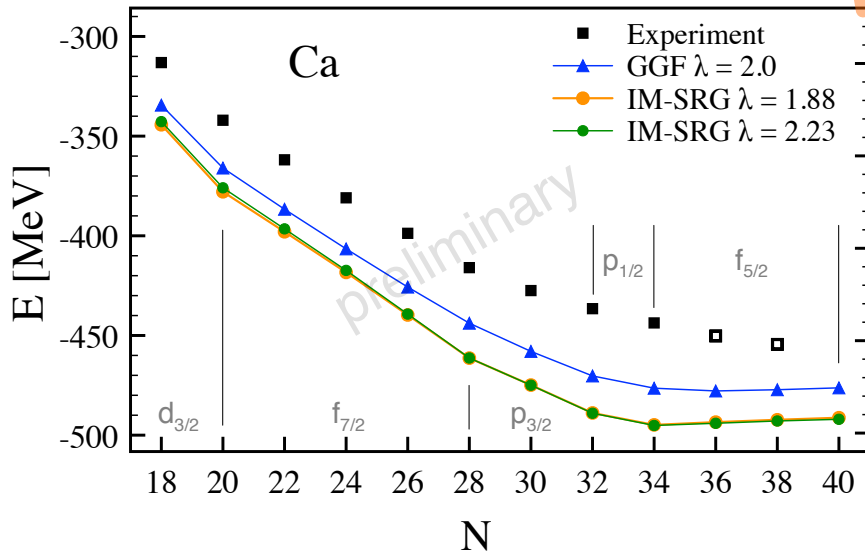


V. Somà, CB *et al.*, in prep.

# Ca and Ni isotopic chains

Calculations based on ramps D, N1, N2:

Preliminary

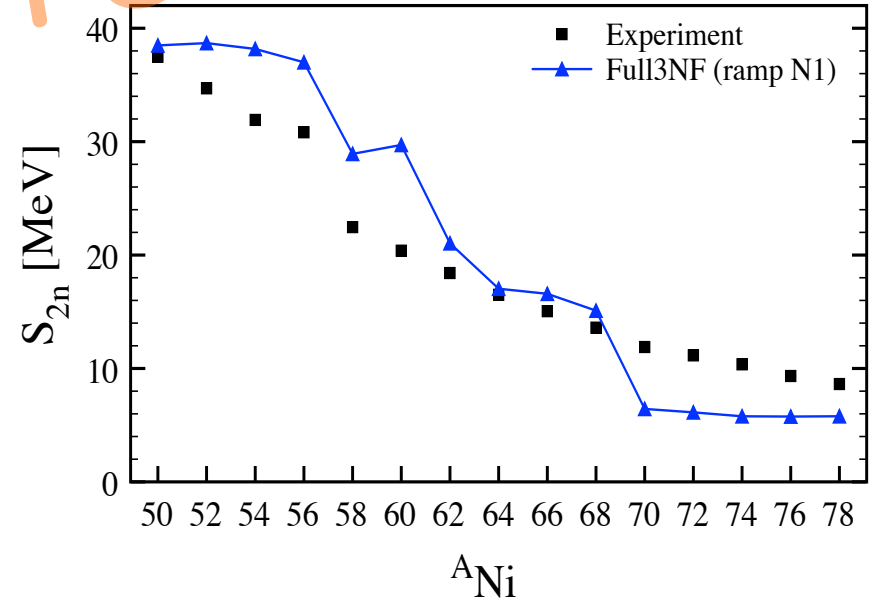
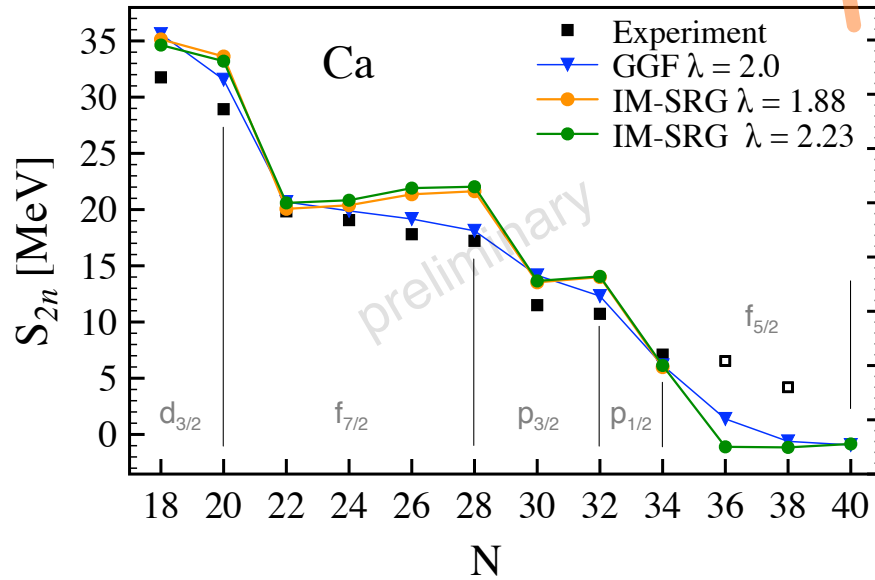


- Large  $J$  in free space SRG matter (must pay attention to its convergence)
- Overall conclusions regarding over binding and  $S_{2n}$  remain but details change

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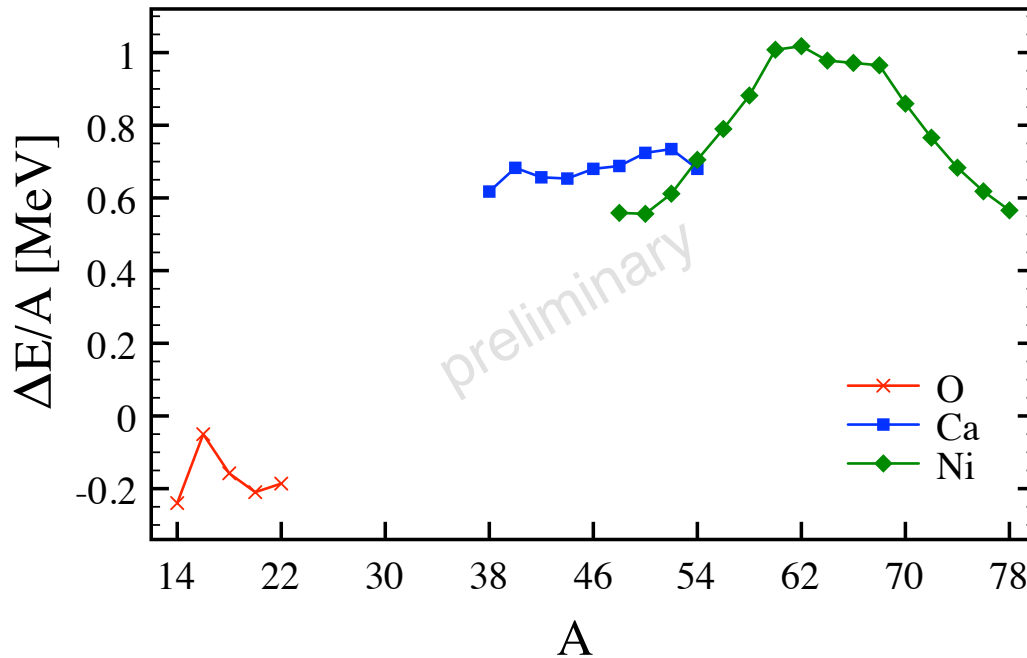


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# Ca and Ni isotopic chains

Difference of calculated BEs to the experiment  
for different masses:

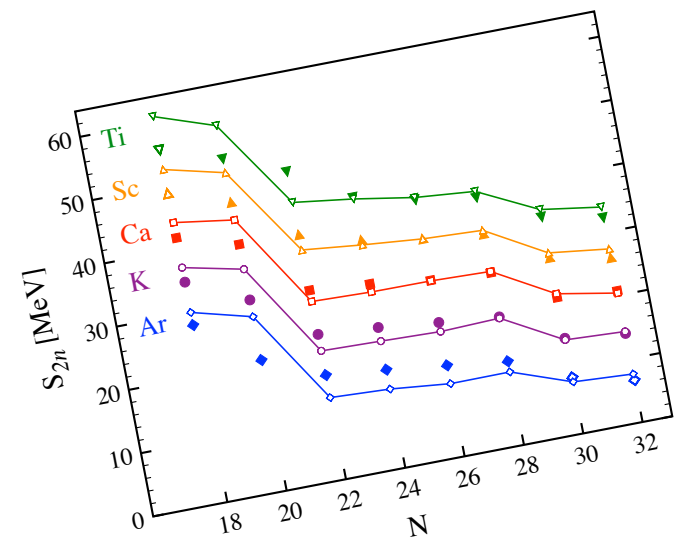


preliminary

→ In general over binding per nucleon ( $E/A$ ) appear to stabilize above  $A \sim 40-50$  but more investigations are required.

# Conclusions

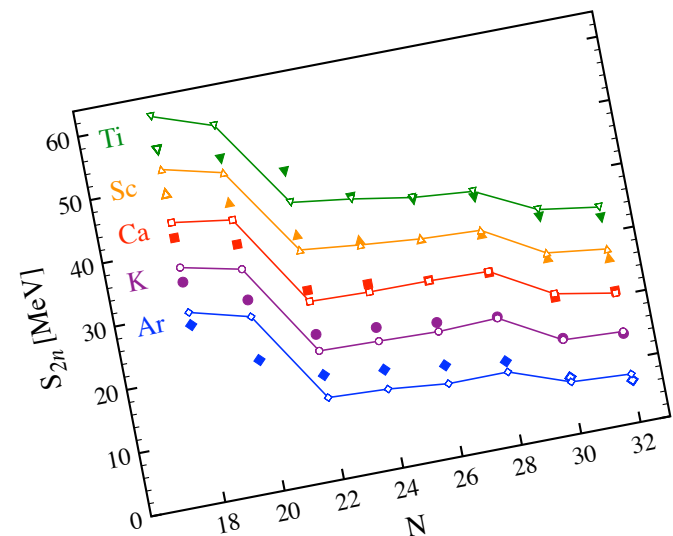
- What to did we learn about realistic chiral forces from ab-initio calculation ?
  - *Leading order 3NF are crucial to predict many important features that are observed experimentally (drip lines, saturation, orbit evolution, etc...)*
  - *Experimental binding is predicted accurately up to the lower sd shell ( $A \approx 30$ ) but deteriorates for medium mass isotopes (Ca and above) with roughly  $1 \text{ MeV}/A$  over binding.*
  - *This hints to the need of more repulsion in future generations of chiral realistic forces.*



# Conclusions

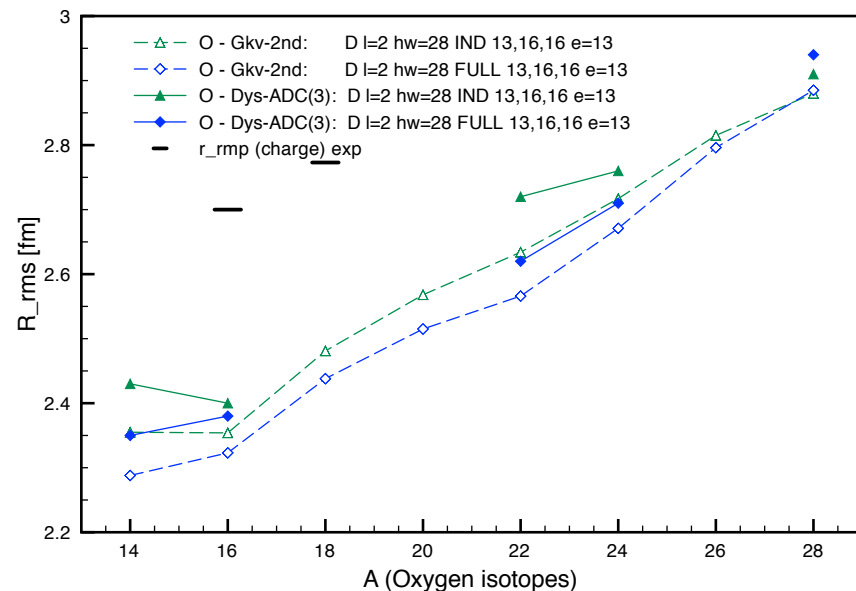
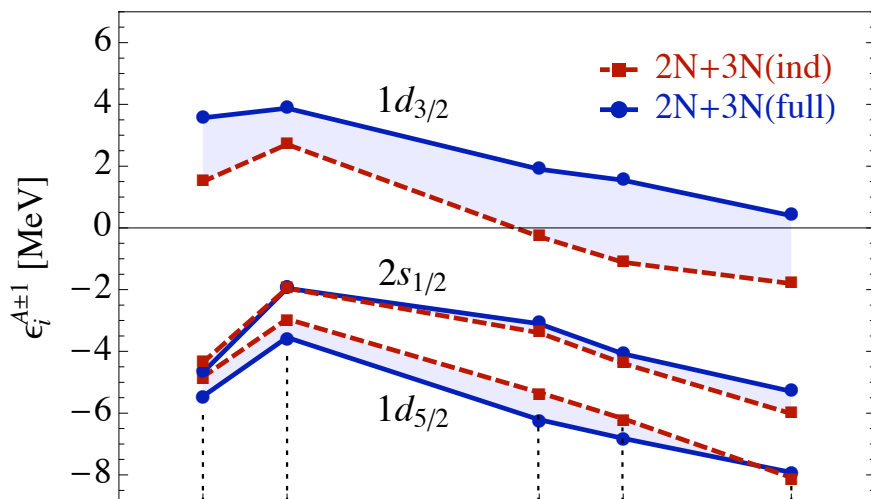
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*Thank you for  
your  
attention!!!*



# Results for the N-O-F chains

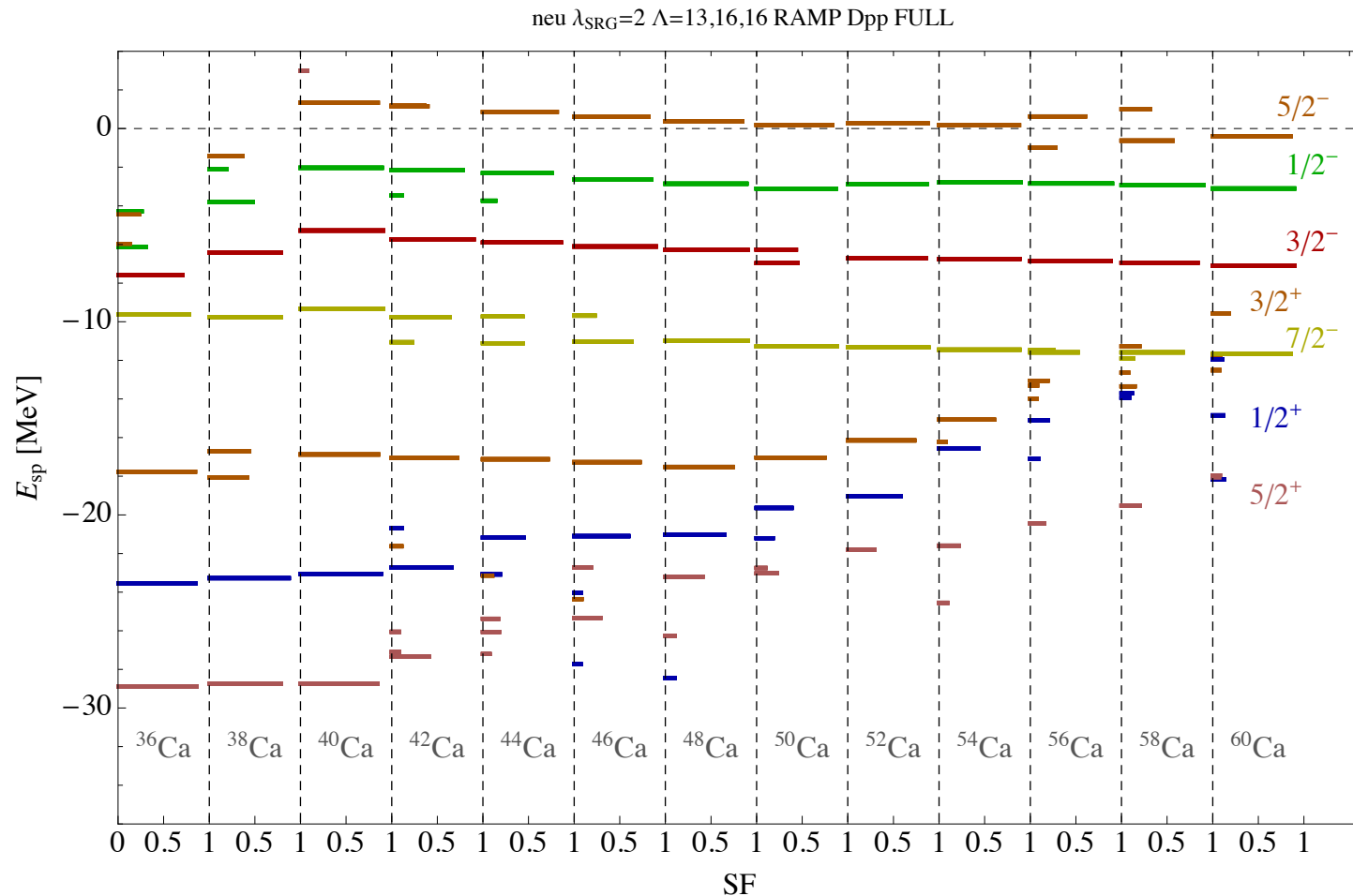
A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)



→ *d3/2* raised by genuine 3NF

→ systematic underestimation of radii

# Ca spectral distributions - at 2<sup>nd</sup> order

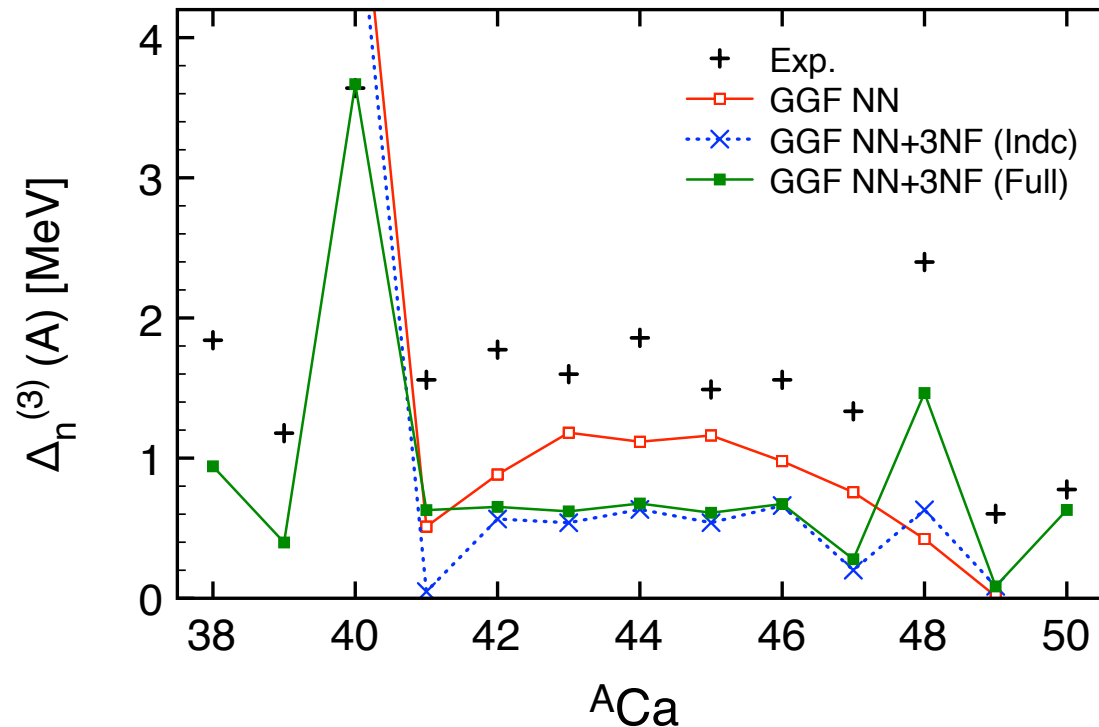


Preliminary

# Pairing gaps

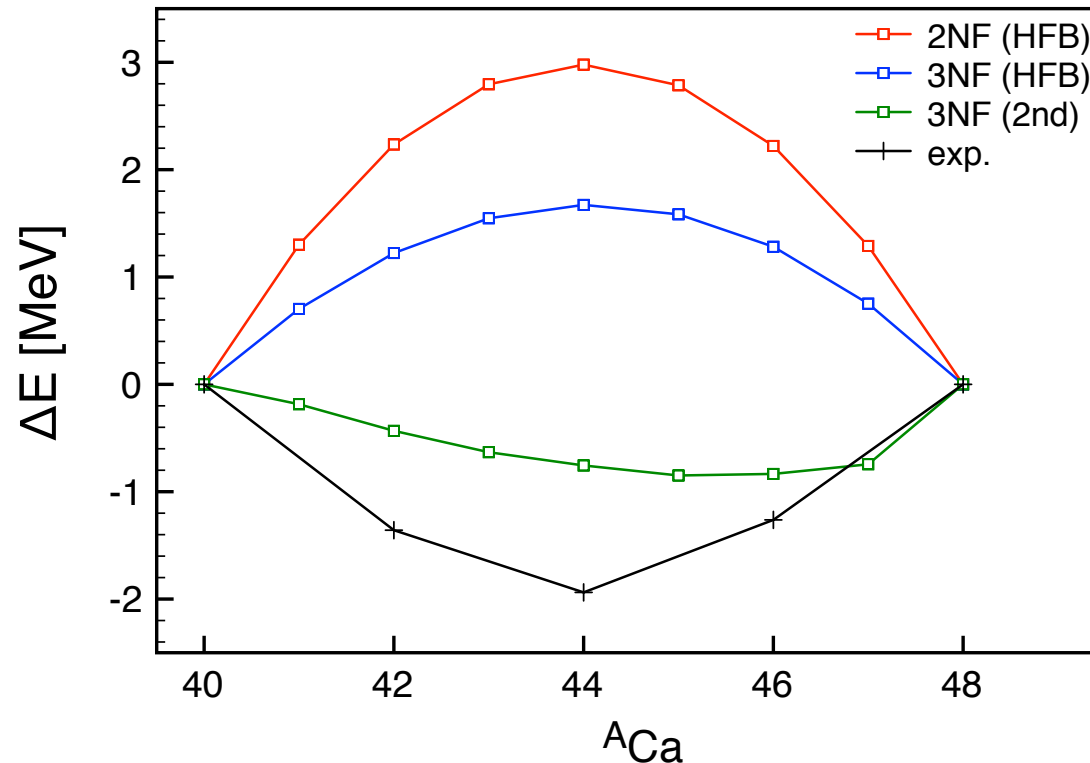
## ★ Three-point mass differences

$$\Delta_n^{(3)}(A) = \frac{(-1)^A}{2} [E_0^{A+1} - 2E_0^A + E_0^{A-1}]$$



# Pairing gaps

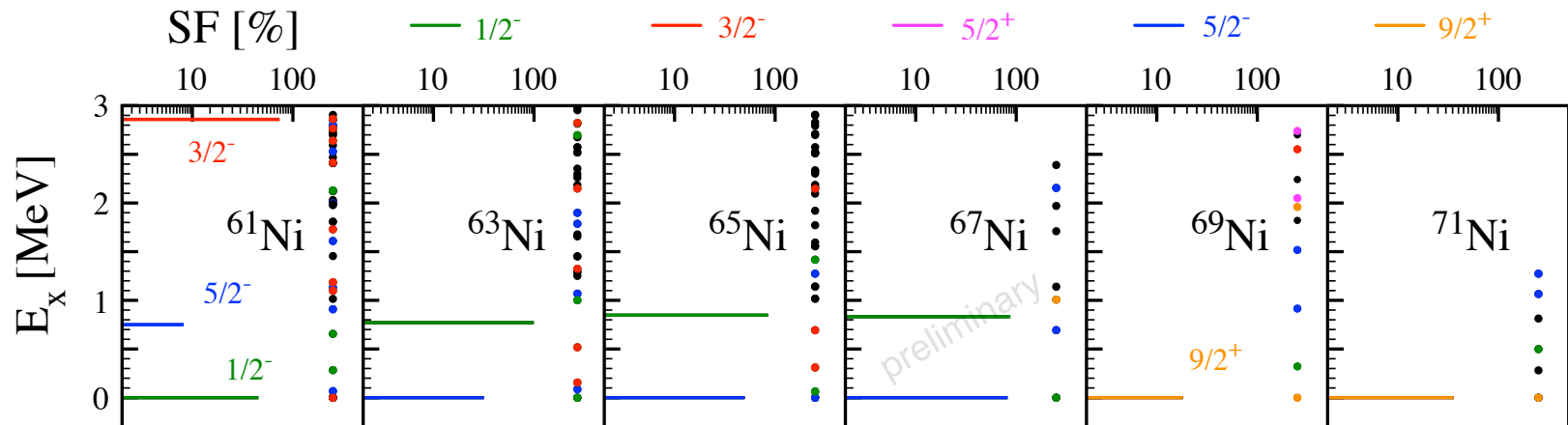
⊛ Inversion of odd-even staggering



⇒ Second order and 3NF necessary to invert the staggering

# Ni spectral distributions - at 2<sup>nd</sup> order

Preliminary





# Collaborators



energies atomiques • énergies alternatives



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DARMSTADT



B Universitat de Barcelona



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*P. Navratil*

*A. Polls*

*W.H. Dickhoff, S. Waldecker*

*D. Van Neck, M. Degroote*

*M. Hjorth-Jensen*